

# Optimized eeeBond: Energy Efficiency with non-Proportional Router Network Interfaces

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# Background and motivation

- Networks provisioned for peak loads
  - Typically very low utilization
  - Opportunity to save energy
- Energy proportionality desirable
  - Energy usage proportional to system utilization
  - However, hardware limitations prevents this in practice
- Two promising approaches
  - EEE: “On/off toggling” of interface
  - eBond: Switch between redundant heterogeneous interfaces

# Contributions

## 1. Present eeeBond

- Hybrid of EEE and eBond



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*EEE* +



	“Always on”	“On/off toggling”
Single interface	Naïve/default	EEE
Multi interface	eBond	eeeBond

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## 1. Present eeeBond

- Hybrid of EEE and eBond

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## 2. Unified analytic model

- Derive closed-form optimized parameter settings for eBond and eeeBond

	“Always on”	“On/off toggling”
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## 2. Unified analytic model

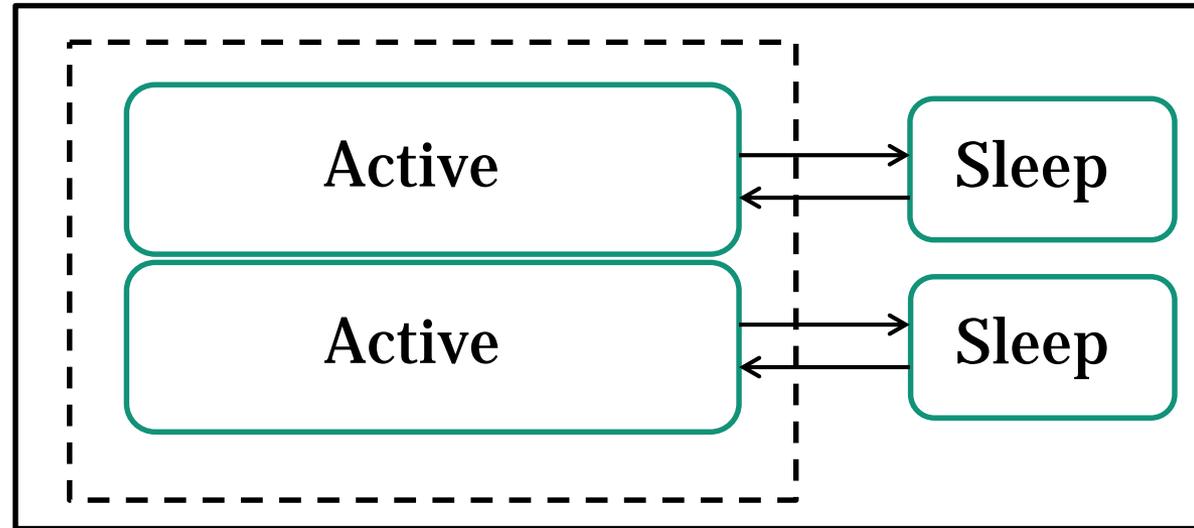
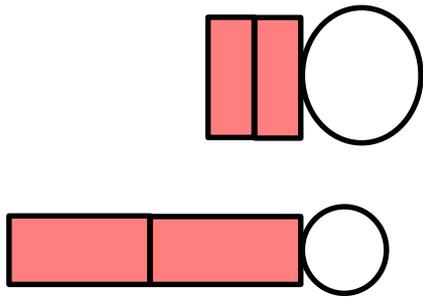
- Derive closed-form optimized parameter settings for eBond and eeeBond

## 3. Performance evaluation

- Characterize gains possible with optimized protocols

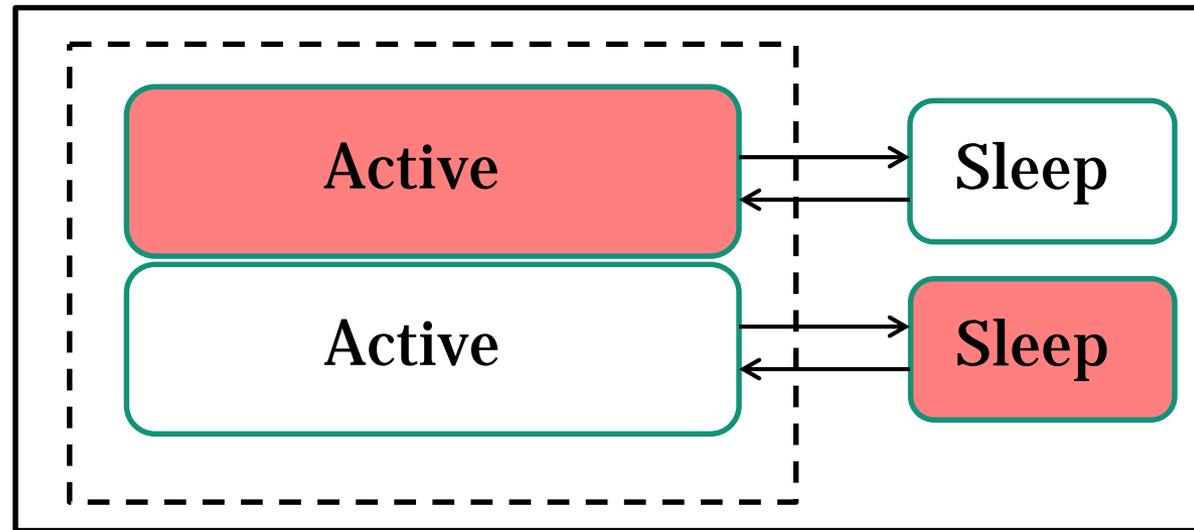
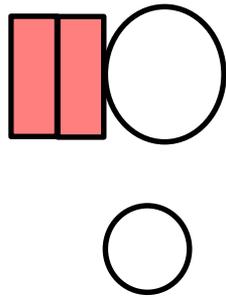
	“Always on”	“On/off toggling”
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# eBond overview



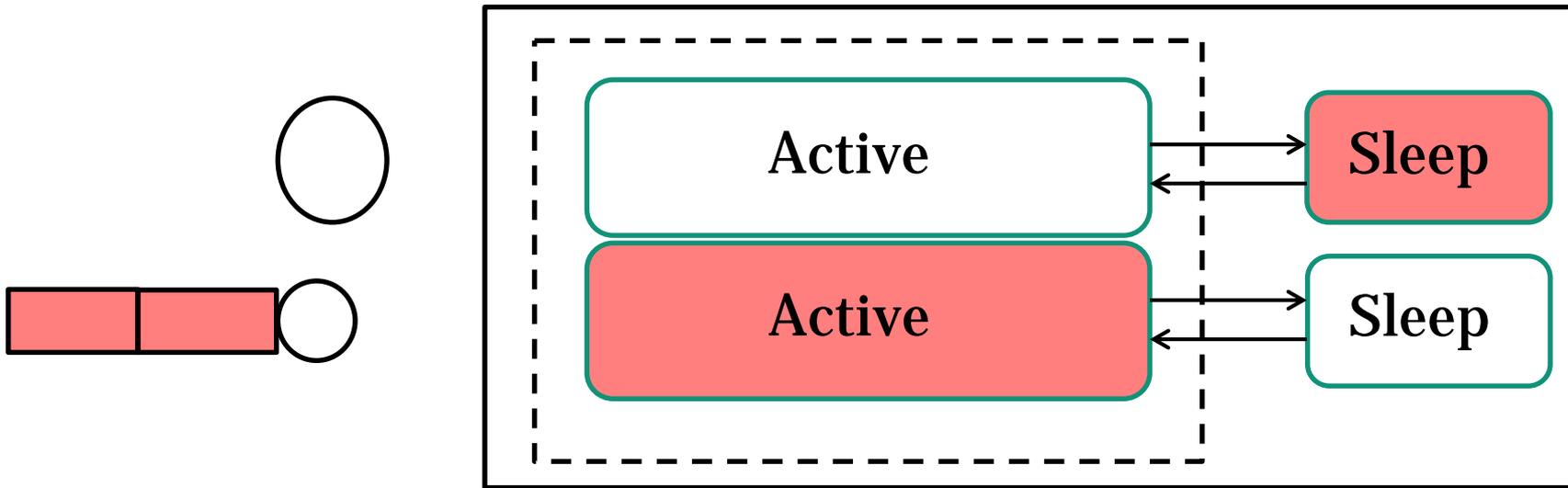
- Redundant heterogeneous interfaces
  - Toggle between interfaces based on load

# eBond overview



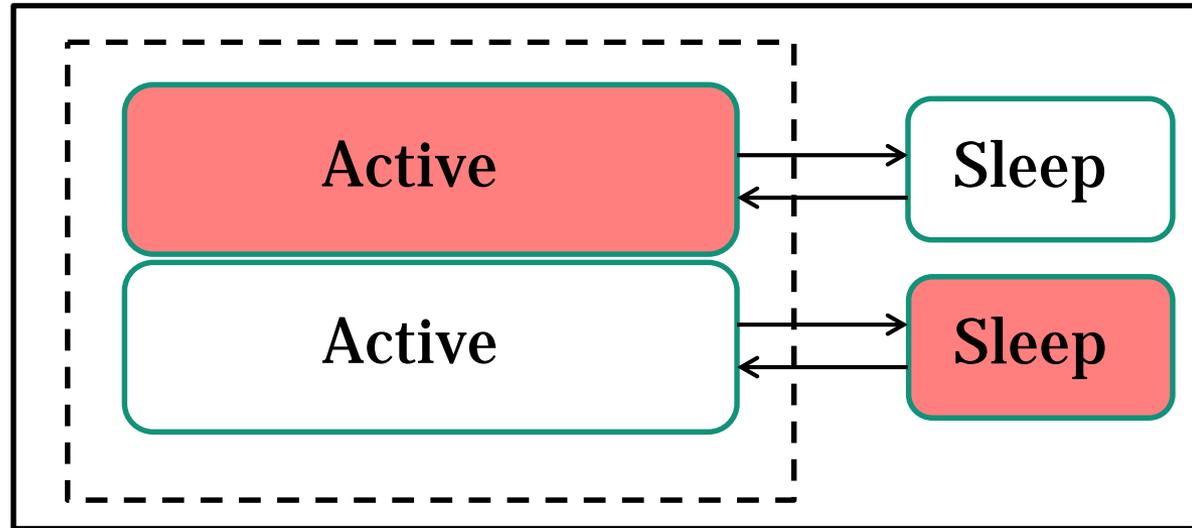
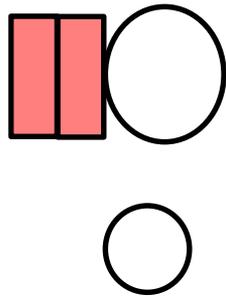
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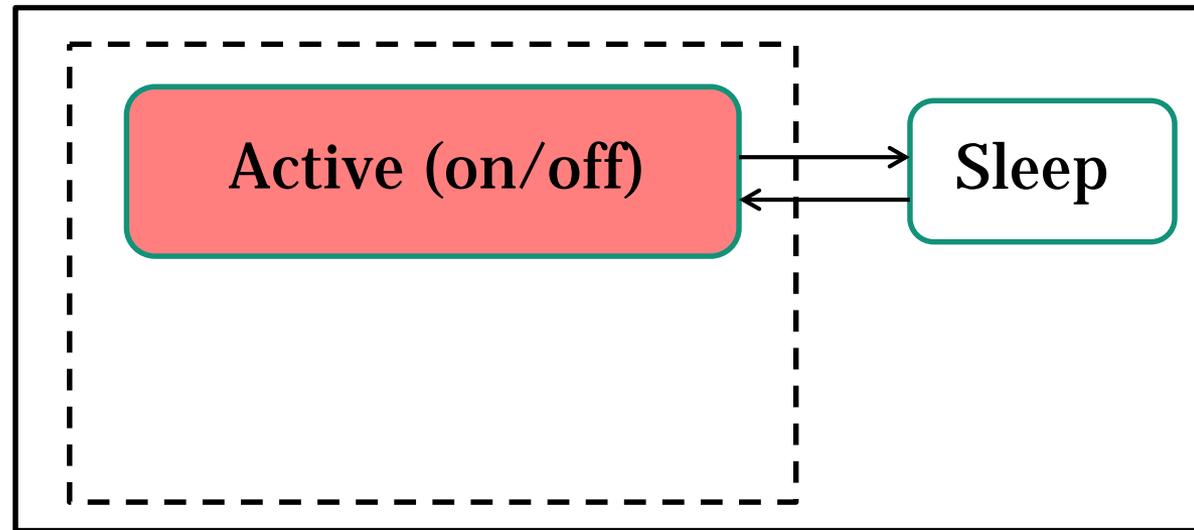
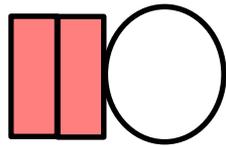
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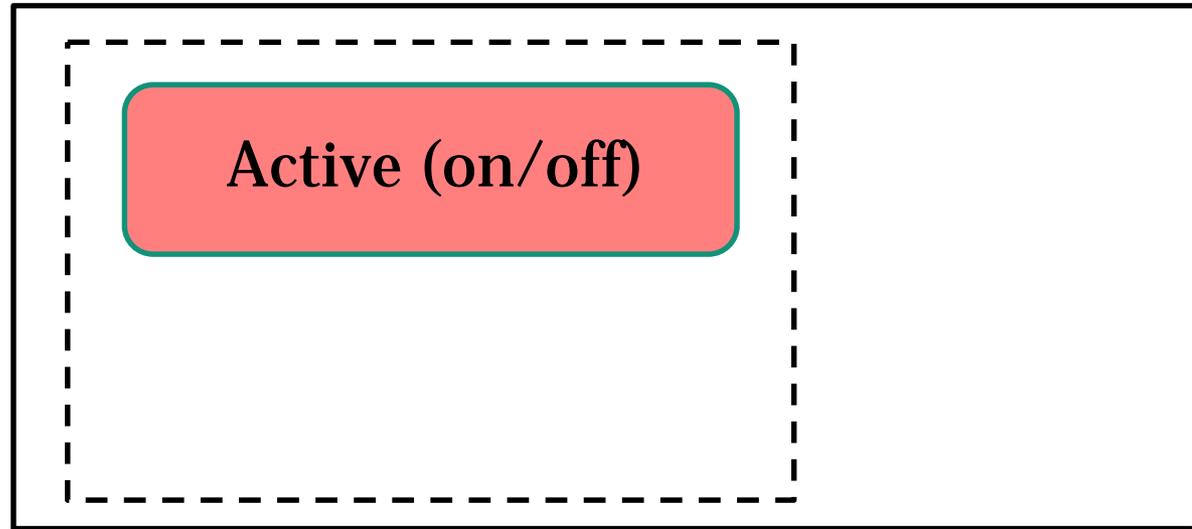
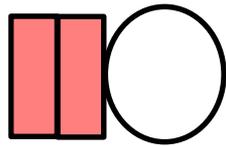
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# EEE overview



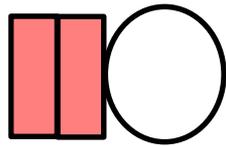
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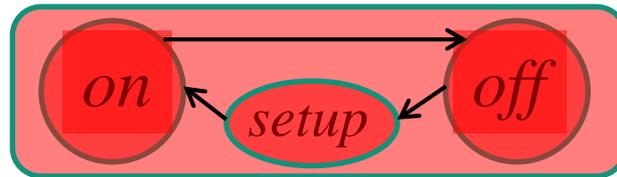
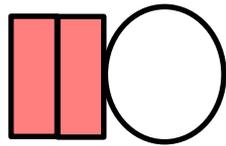
# EEE overview



Active (on/off)

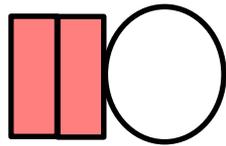
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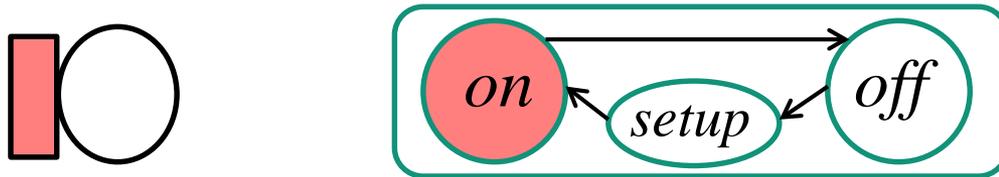
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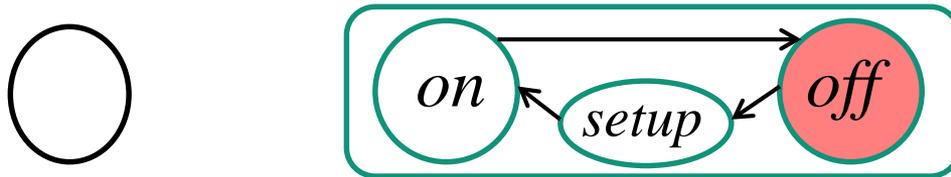
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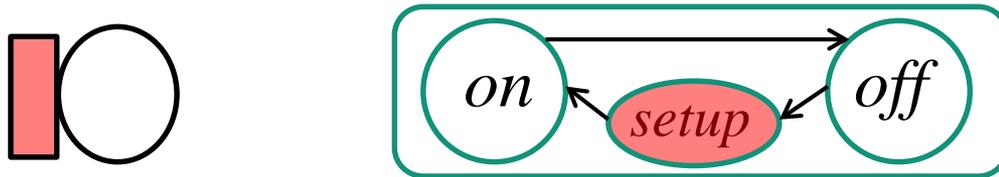
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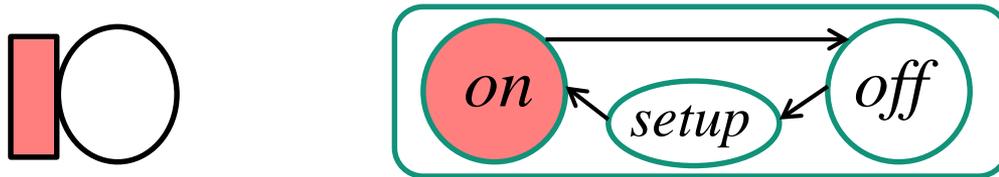
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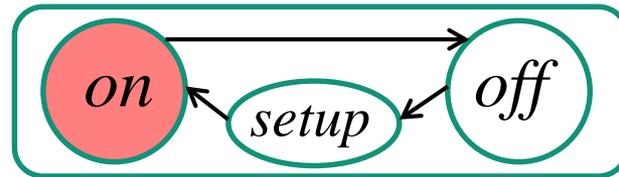
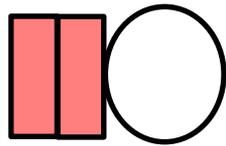
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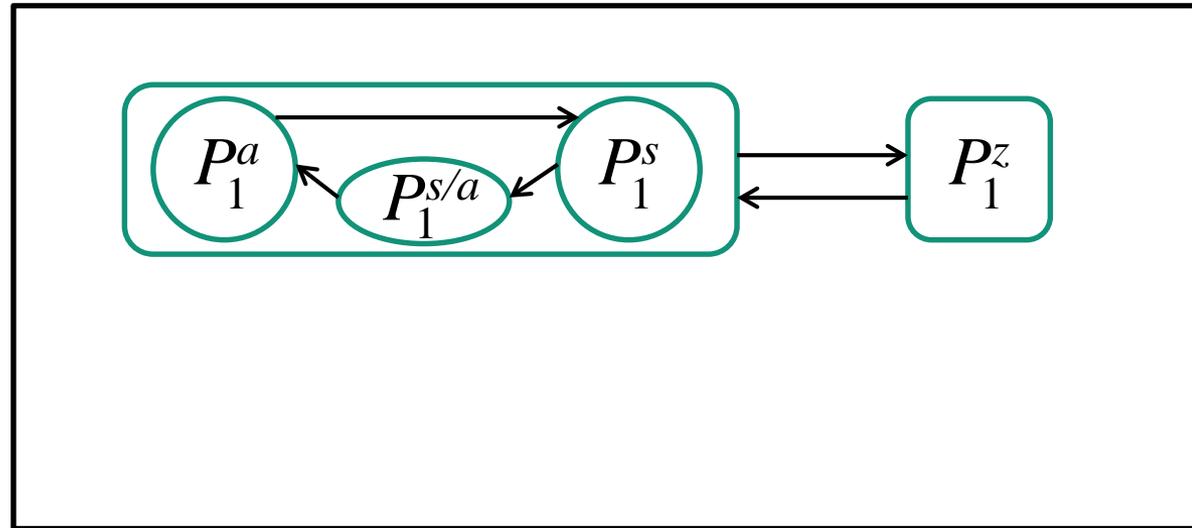
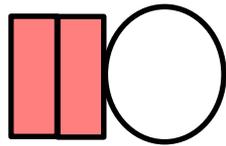
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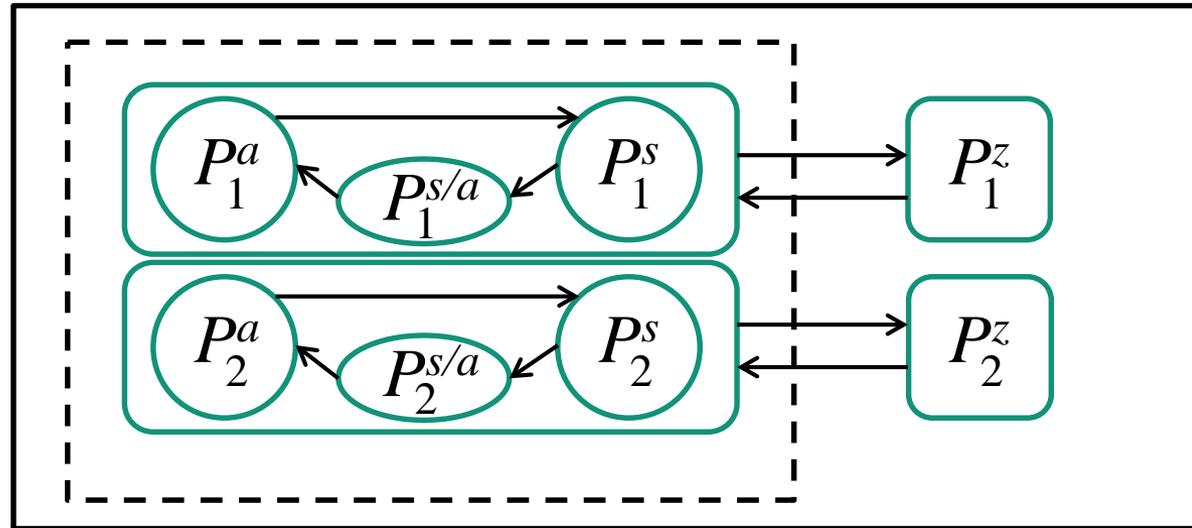
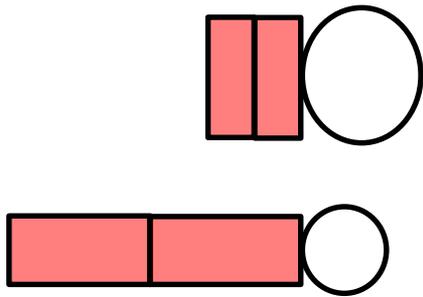
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# Router model and power states

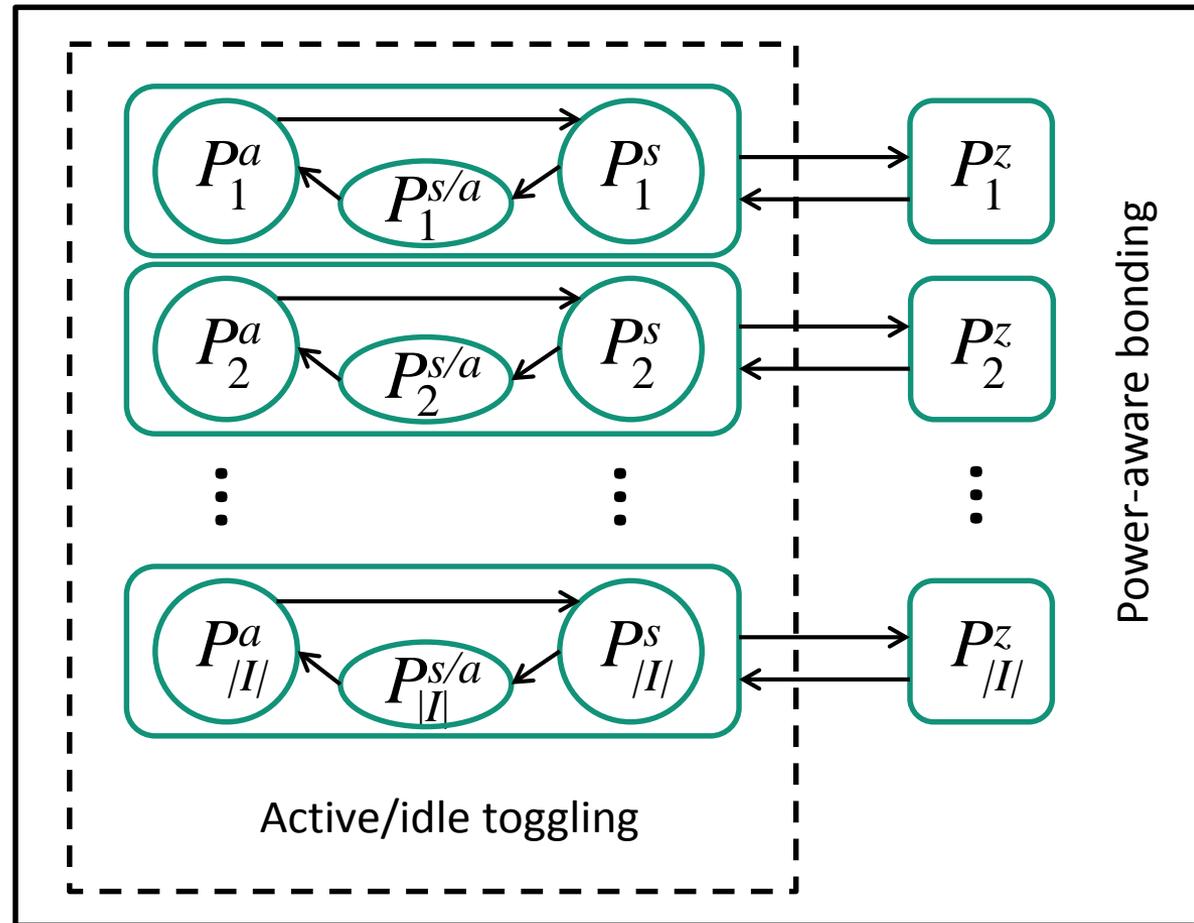
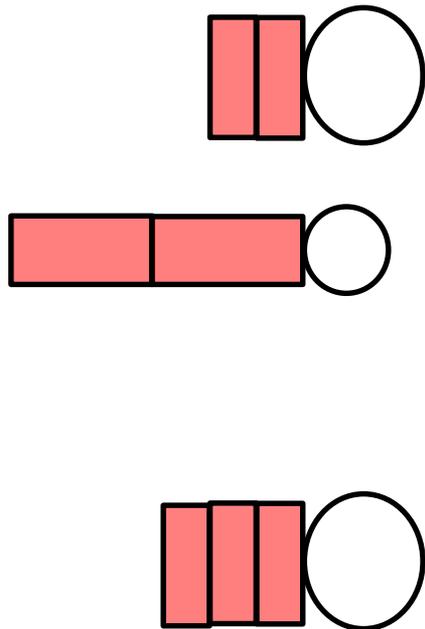


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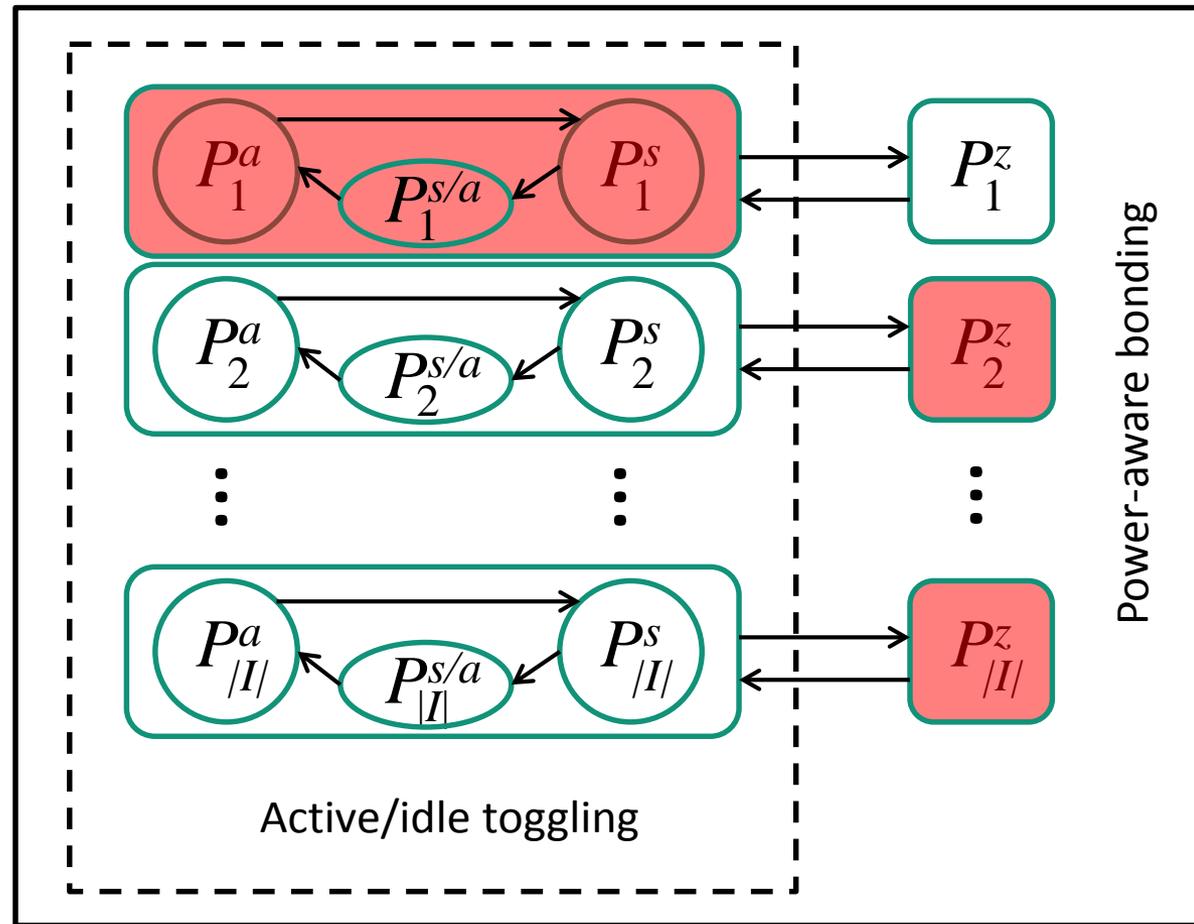
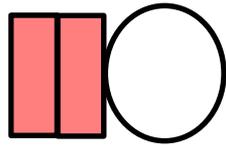
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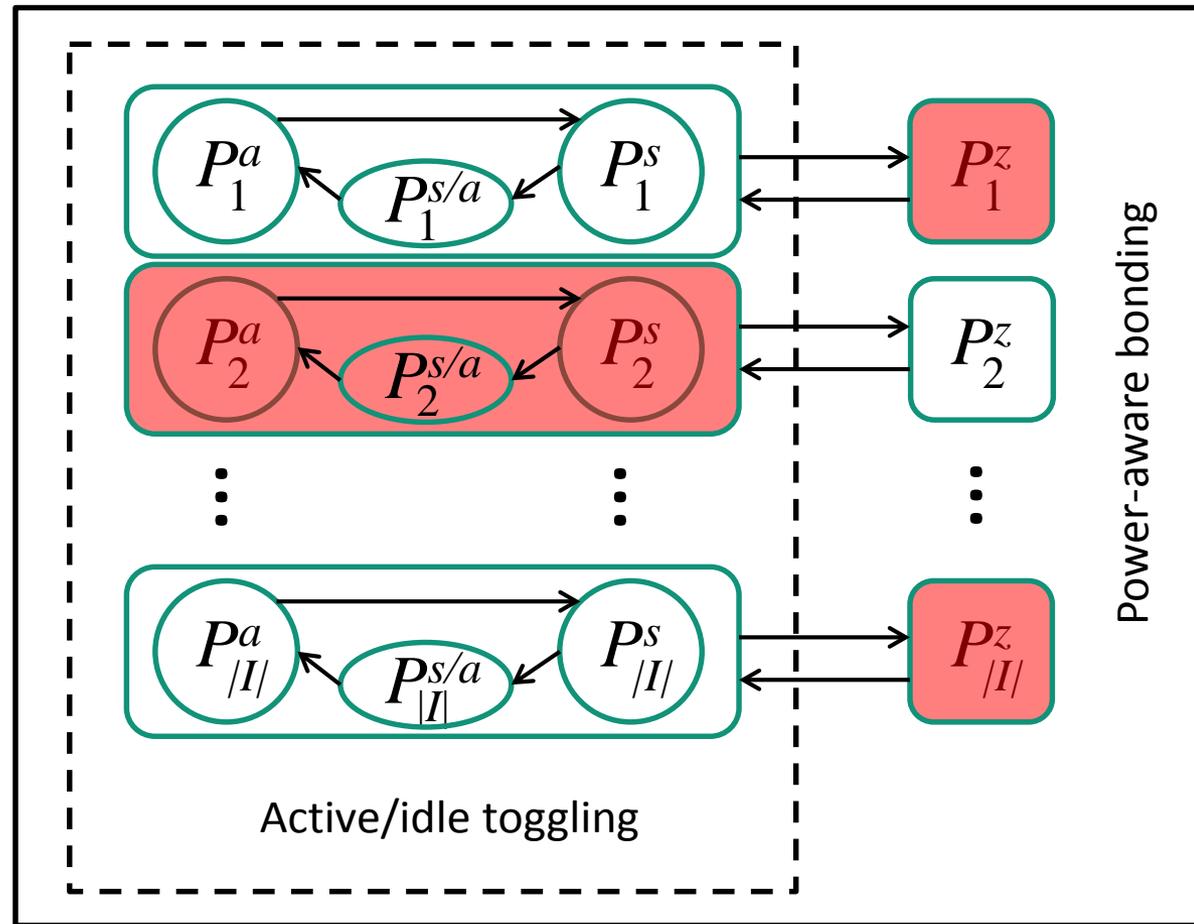
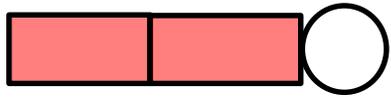
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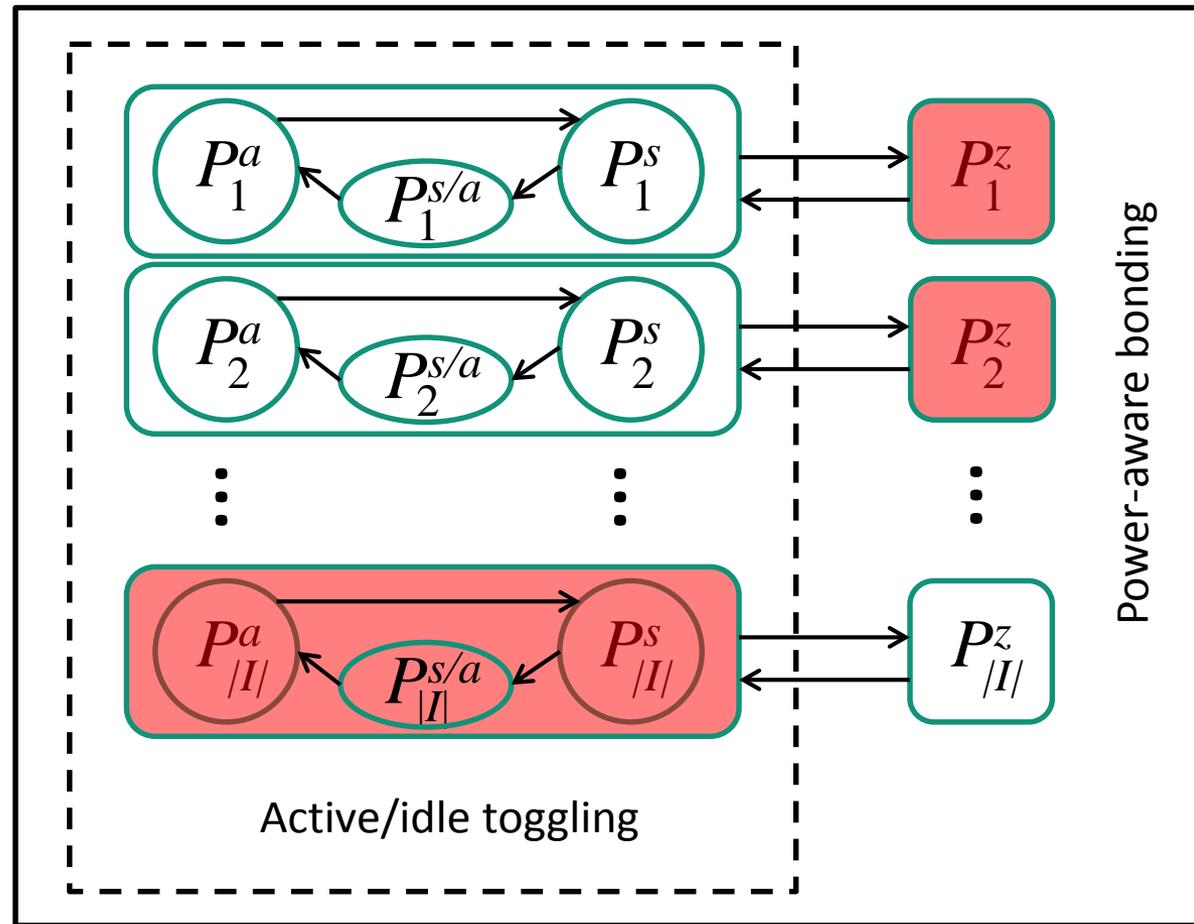
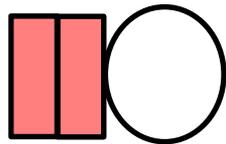
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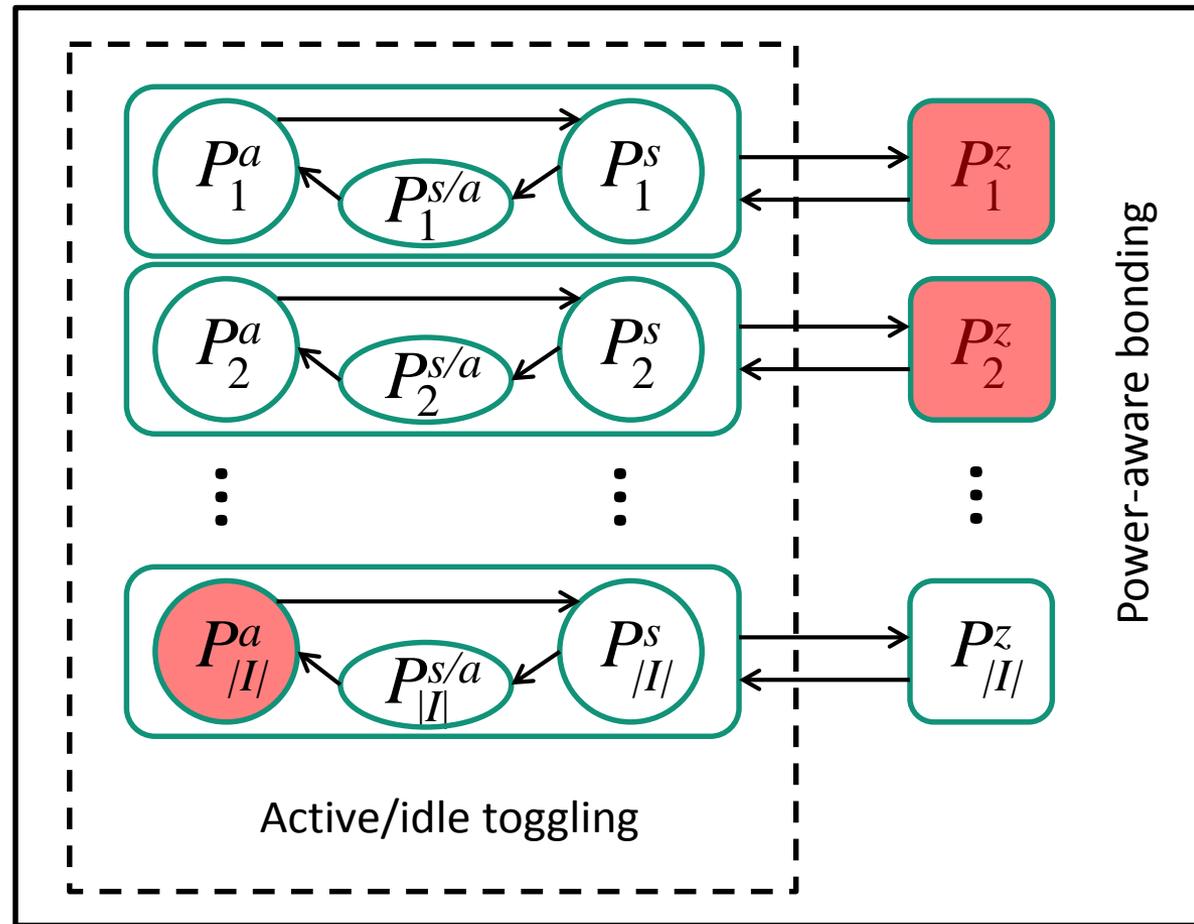
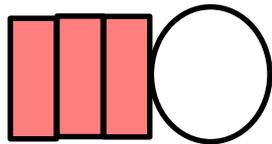
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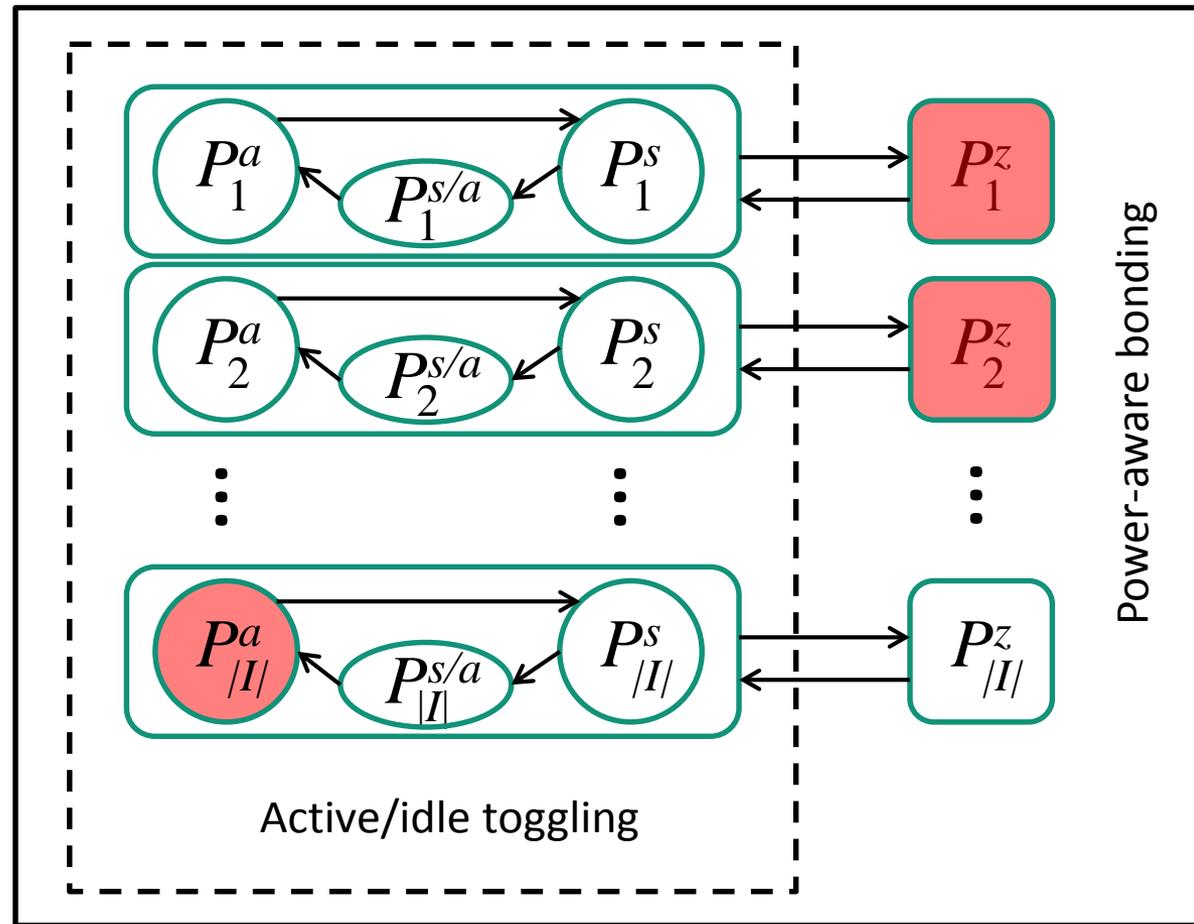
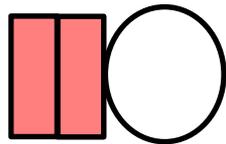
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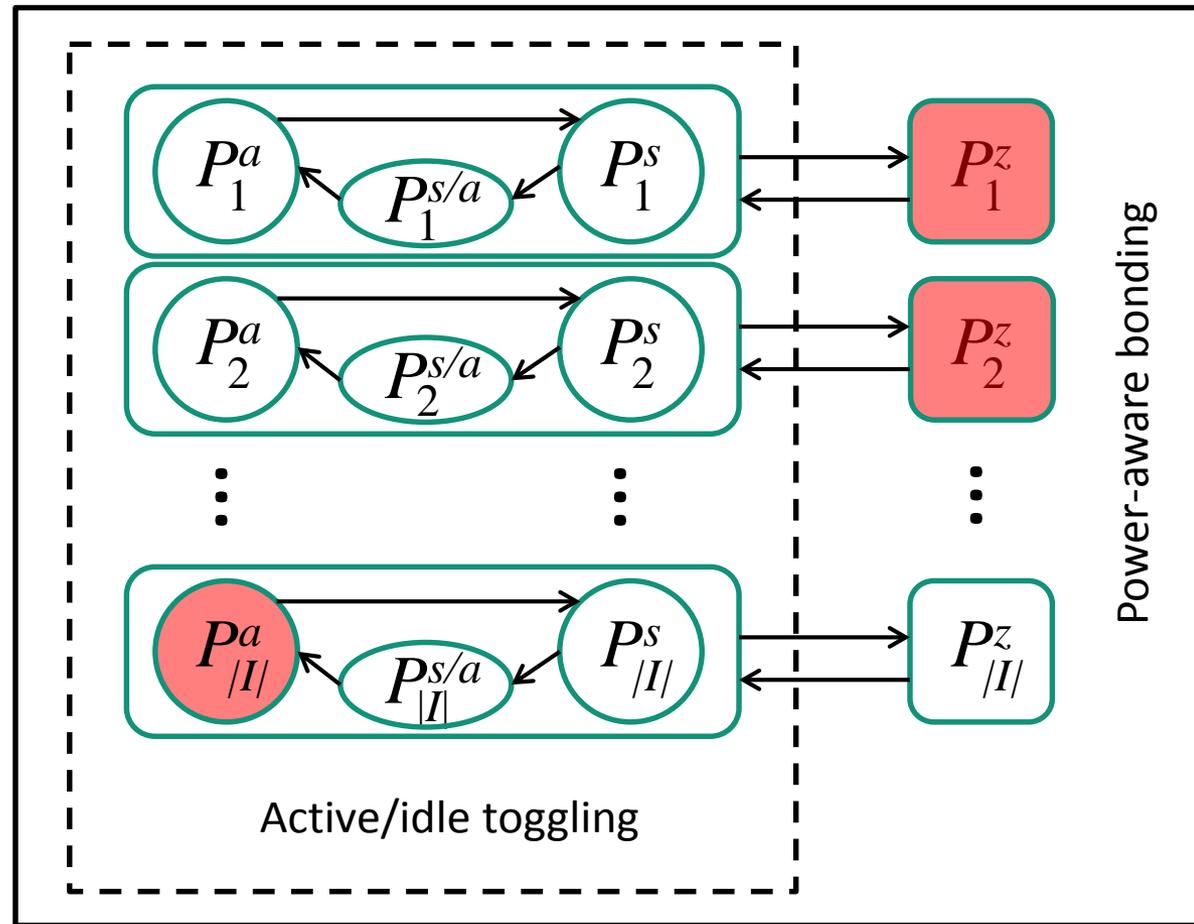
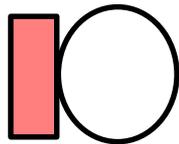
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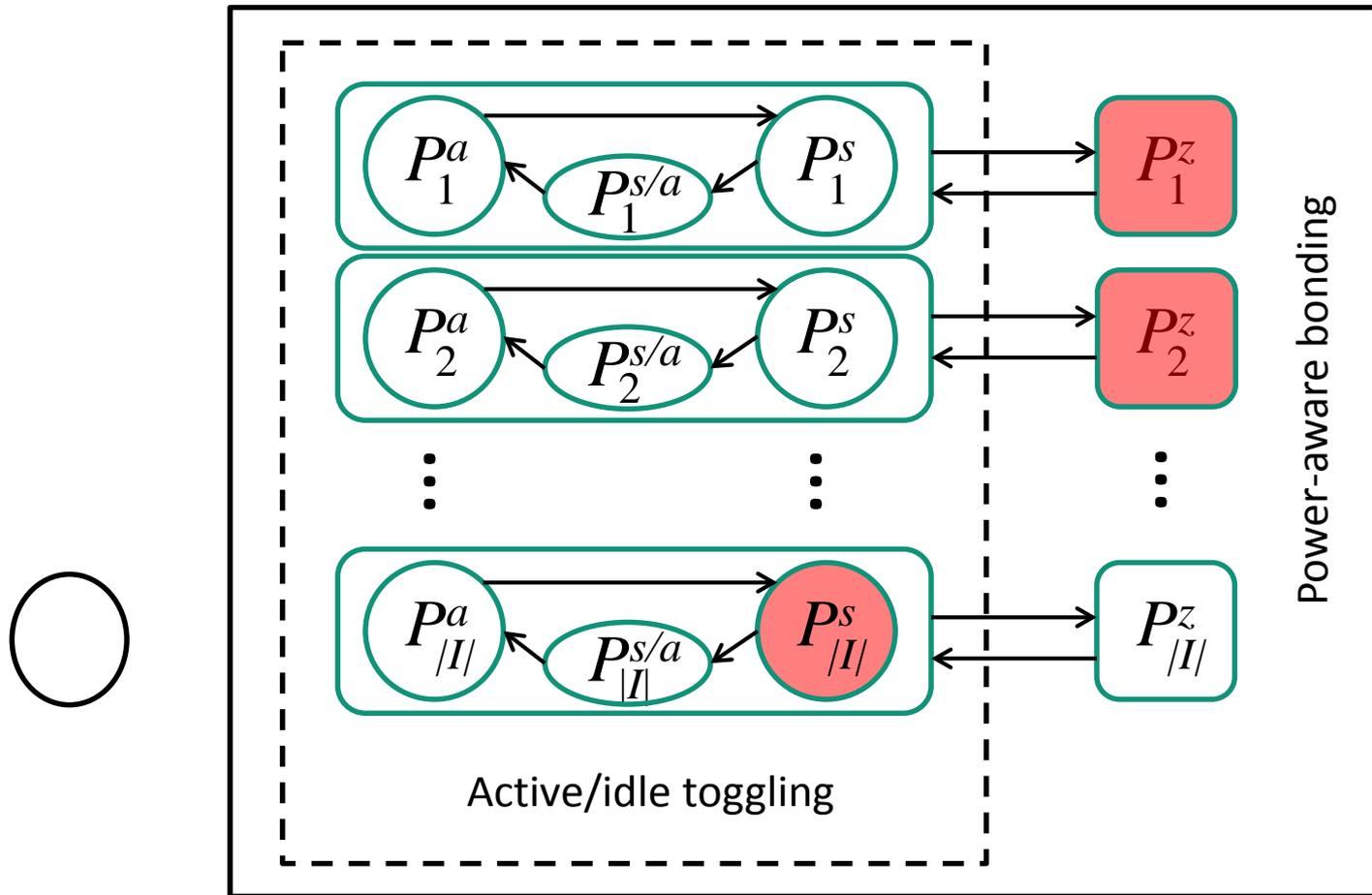
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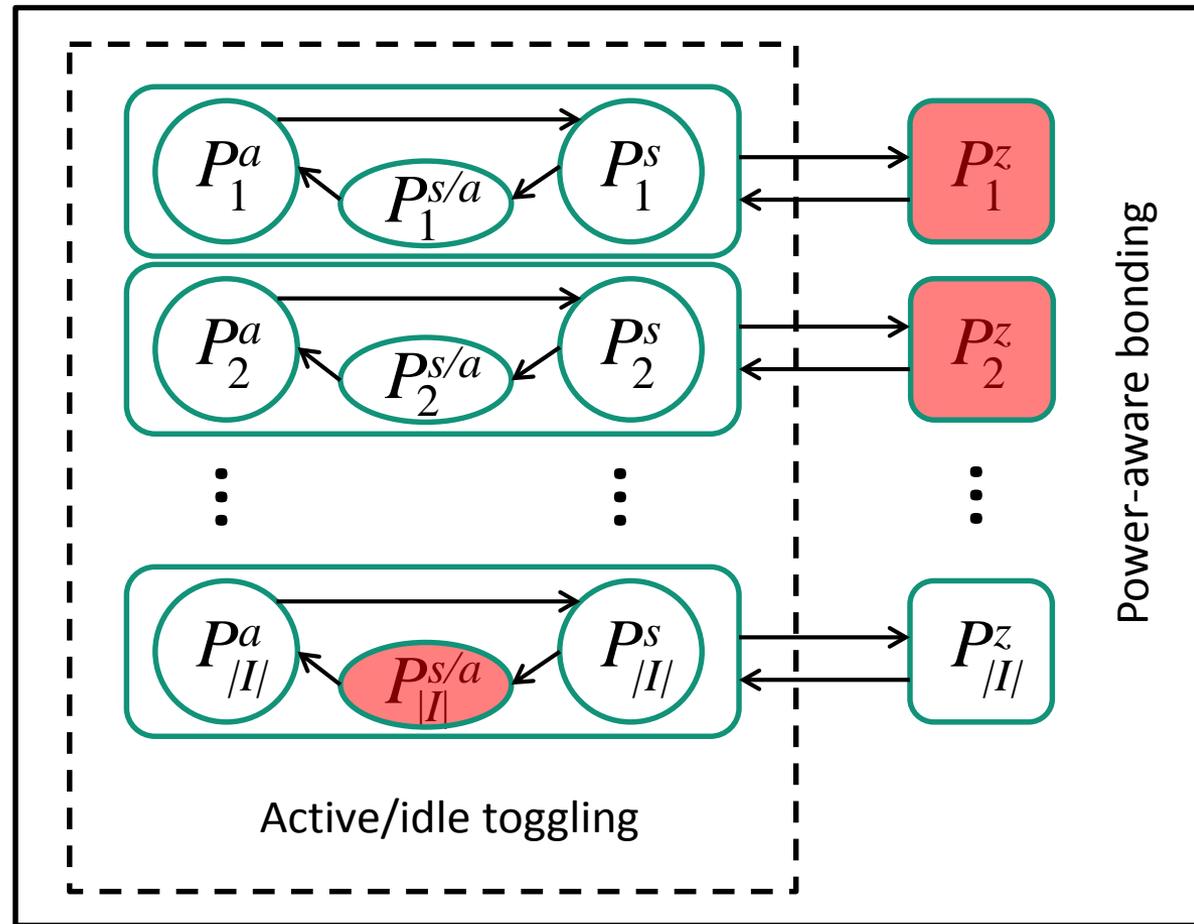
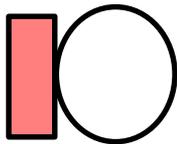
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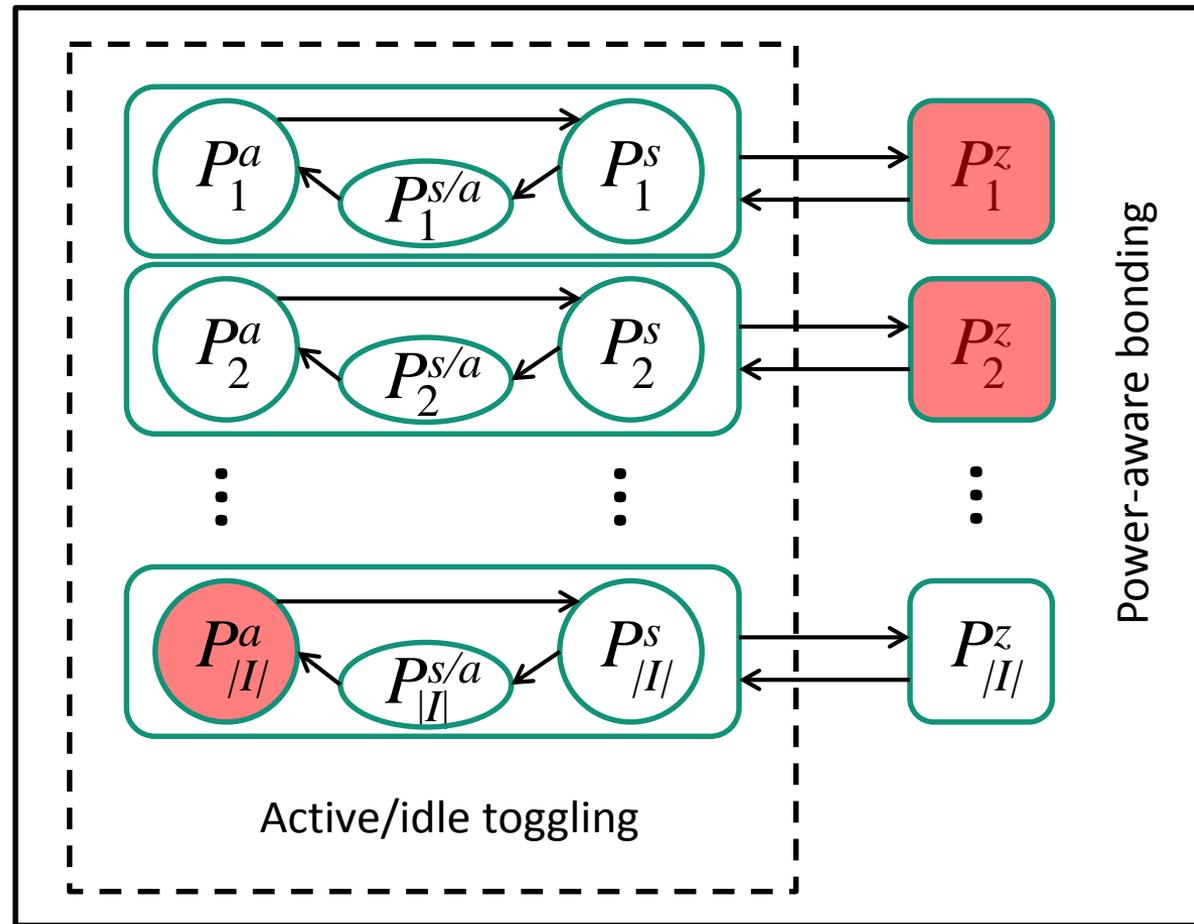
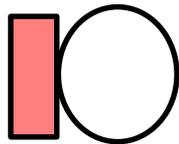
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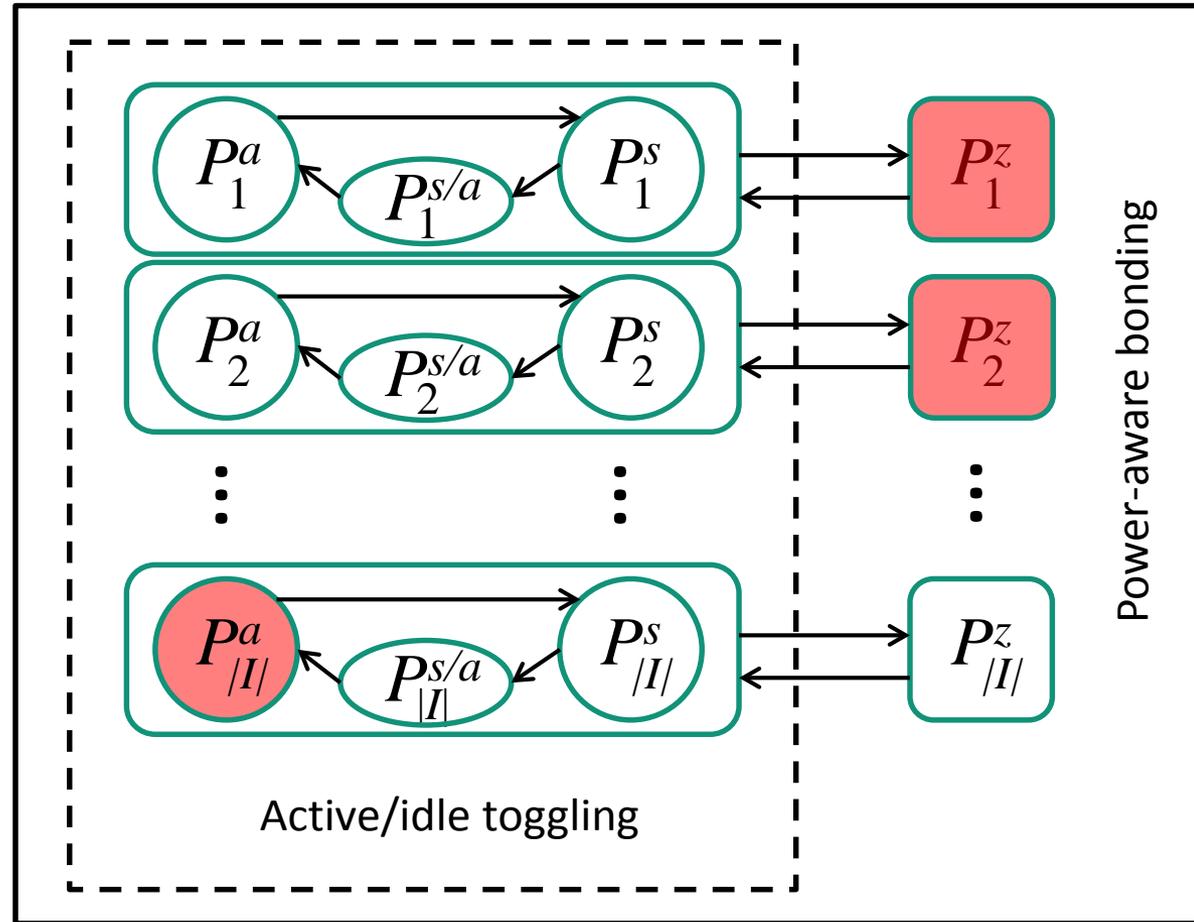
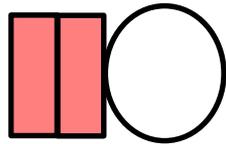
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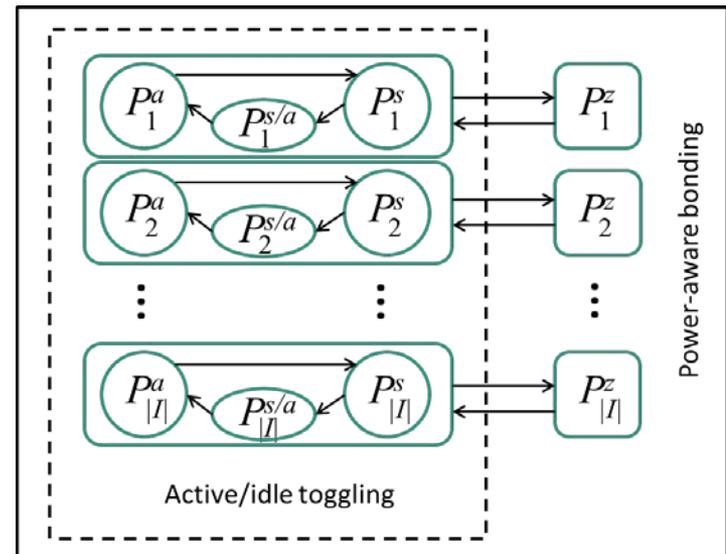
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# General model

- Energy usage

$$P_{\mathcal{I}} = \sum_{i \in \mathcal{I}} \left[ q_i^a P_i^a + q_i^s P_i^s + q_i^{s/a} P_i^{s/a} + q_i^z P_i^z \right].$$

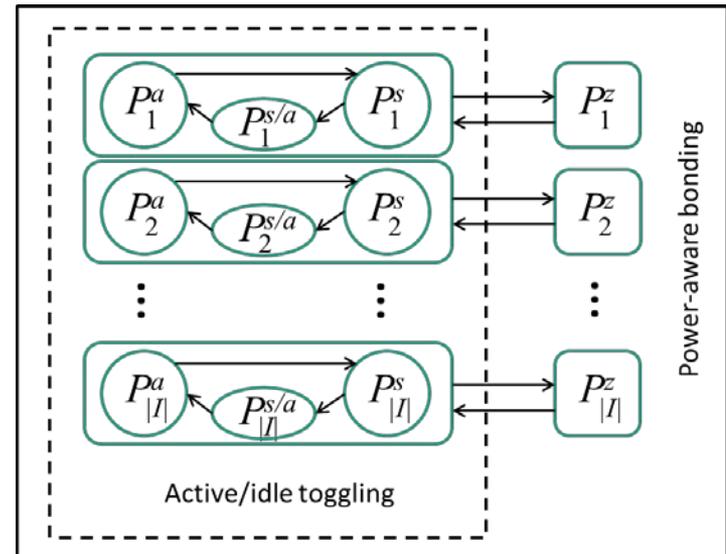


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Sum over all interfaces



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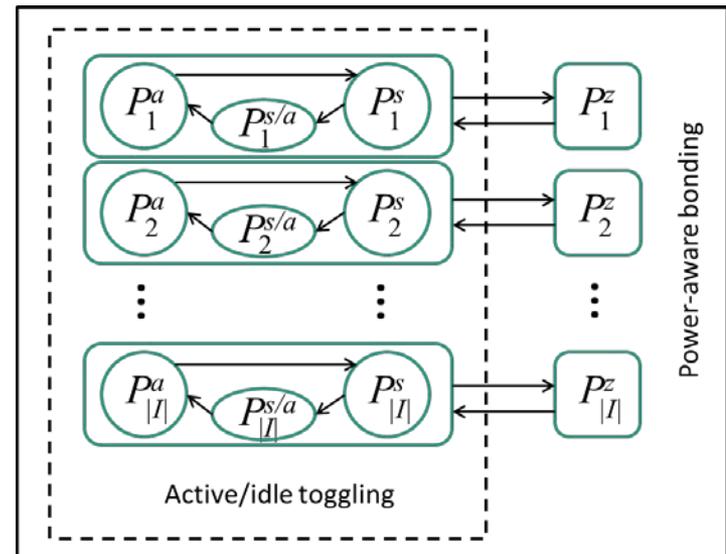
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Active high-power

Short-term sleep

Short setup period

Long-term sleep



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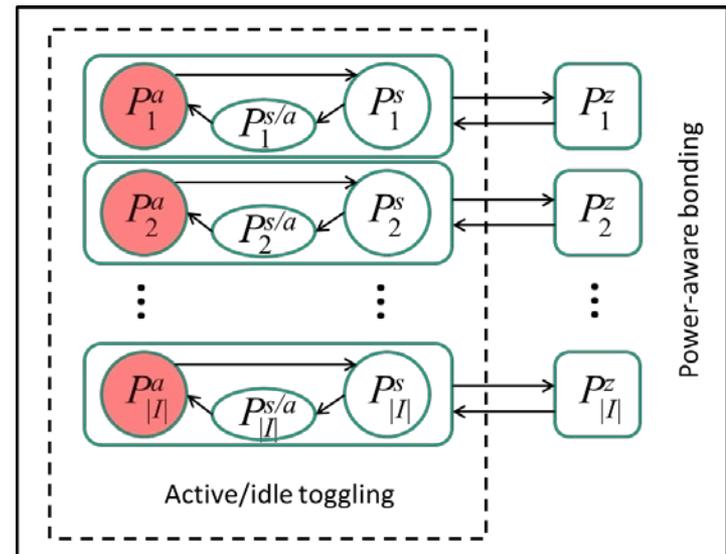
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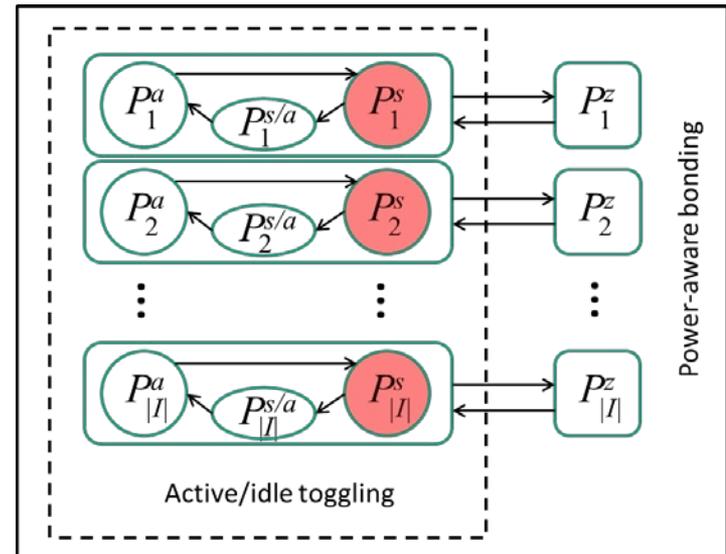
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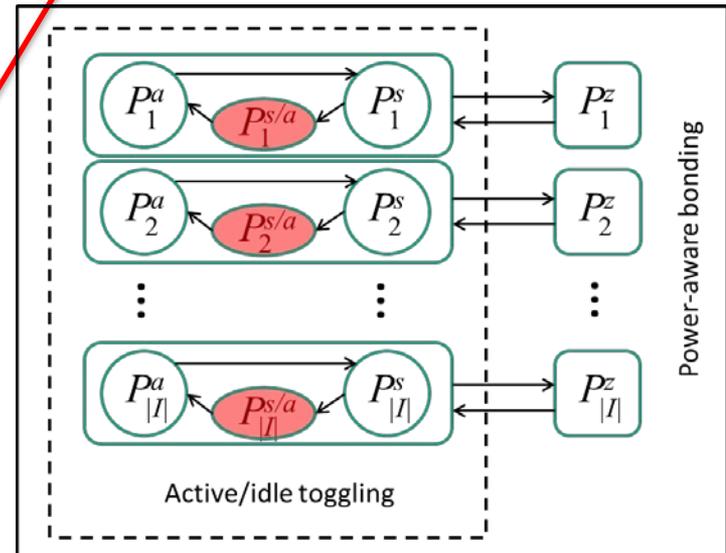
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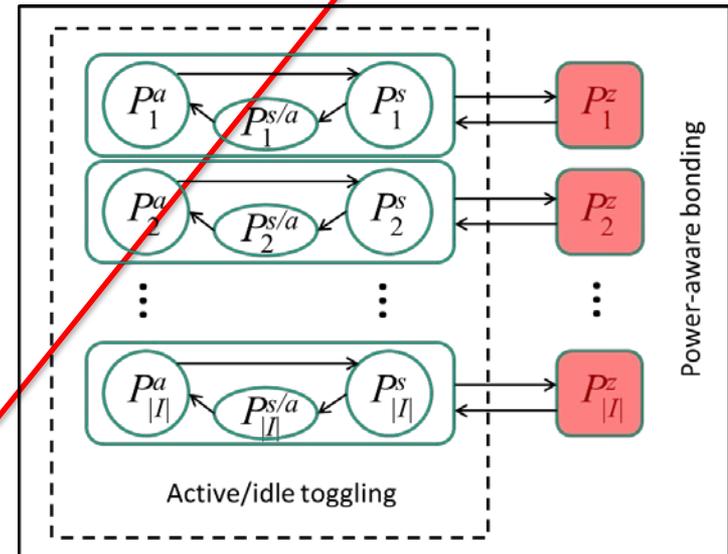
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- Hardware comparison

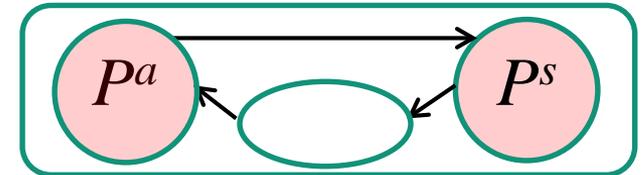
- Per-interface modes:  $c_i = \frac{P_i^s}{P_i^a}$  ( $0 \leq c_i \leq 1$ )     $g_i = \frac{P_i^{s/a}}{P_i^a}$   $g_i \approx 1$
- Interface differences:  $P_i^a = f(\mu_i)$ , where  $f(\mu_i) = P_0^a \left(\frac{\mu_i}{\mu_0}\right)^x$

# General model

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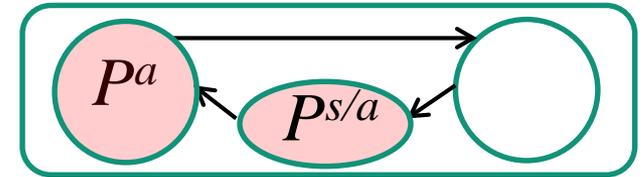


## Sleep savings ratio

- Hardware comparison

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# General model



Setup power

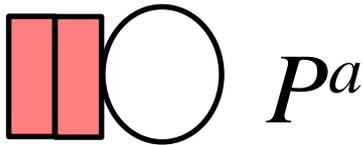
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**Power scaling between interfaces**

# General model

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- **Per-interface delay**

- **Setup time:**

$$w_k = \begin{cases} \Delta_i + \frac{l_k}{\mu_i}, & \text{if } t_k > t_{k-1} + w_{k-1} \\ w_{k-1} + t_{k-1} - t_k + \frac{l_k}{\mu_i}, & \text{otherwise.} \end{cases}$$

# General model

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# General model

Setup time + service time

If arriving to empty system

- Per-interface delay
  - Setup time:

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# General model

**Time stuck behind earlier packet + service time**

**If arriving to “busy” system**

- Per-interface delay
  - Setup time:

$$w_k = \begin{cases} \Delta_i + \frac{l_k}{\mu_i} & \text{if } t_k > t_{k-1} + w_{k-1} \\ w_{k-1} + t_{k-1} - t_k + \frac{l_k}{\mu_i} & \text{otherwise.} \end{cases}$$

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- Per-interface delay

- Setup time:

$$w_k = \begin{cases} \Delta_i + \frac{l_k}{\mu_i}, & \text{if } t_k > t_{k-1} + w_{k-1} \\ w_{k-1} + t_{k-1} - t_k + \frac{l_k}{\mu_i}, & \text{otherwise.} \end{cases}$$

# Steady-state model

- M/G/1(E,SU) model
- Waiting times

$$\overline{W}_i = E[w_k | i] = \frac{\lambda E[S_i^2]}{2(1 - \rho_i)} + \frac{2E[\Delta_i] + \lambda E[\Delta_i^2]}{2(1 + \lambda E[\Delta_i])},$$

- Energy usage of active interfaces

$$\frac{P_i - q_i^z P_i^z}{1 - q_i^z} = \left[ \rho_i P_i^a + \frac{1 - \rho_i}{1 + \lambda E[\Delta_i]} P_i^s + \frac{\lambda(1 - \rho) E[\Delta_i]}{1 + \lambda E[\Delta_i]} P_i^{s/a} \right]$$

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- M/G/1(E,SU) model
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**M/G/1 without vacations**

# Steady-state model

- M/G/1(E,SU) model
- Waiting times

$$\bar{W}_i = E[w_k | i] = \frac{\lambda E[S_i^2]}{2(1 - \rho_i)} - \frac{2E[\Delta_i] + \lambda E[\Delta_i^2]}{2(1 + \lambda E[\Delta_i])},$$

**M/G/1 without vacations**

**Setup delay penalty**

# Steady-state model

- M/G/1(E,SU) model
- Waiting times

$$\overline{W}_i = E[w_k | i] = \frac{\lambda E[S_i^2]}{2(1 - \rho_i)} + \frac{2E[\Delta_i] + \lambda E[\Delta_i^2]}{2(1 + \lambda E[\Delta_i])},$$

- Energy usage of active interfaces

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Average power usage, conditioned on “active”

# Steady-state model

- Energy usage of active interfaces

$$\frac{P_i - q_i^z P_i^z}{1 - q_i^z} = \left[ \rho_i P_i^a + \frac{1 - \rho_i}{1 + \lambda E[\Delta_i]} P_i^s + \frac{\lambda(1 - \rho) E[\Delta_i]}{1 + \lambda E[\Delta_i]} P_i^{s/a} \right]$$

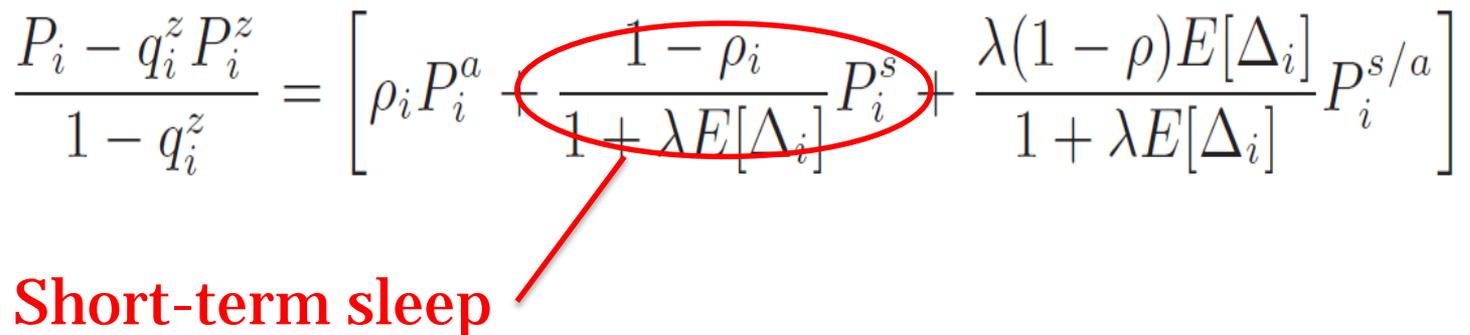
Active high-power

# Steady-state model

- Energy usage of active interfaces

$$\frac{P_i - q_i^z P_i^z}{1 - q_i^z} = \left[ \rho_i P_i^a + \frac{1 - \rho_i}{1 + \lambda E[\Delta_i]} P_i^s + \frac{\lambda(1 - \rho) E[\Delta_i]}{1 + \lambda E[\Delta_i]} P_i^{s/a} \right]$$

**Short-term sleep**



# Steady-state model

- Energy usage of active interfaces

$$\frac{P_i - q_i^z P_i^z}{1 - q_i^z} = \left[ \rho_i P_i^a + \frac{1 - \rho_i}{1 + \lambda E[\Delta_i]} P_i^s + \frac{\lambda(1 - \rho) E[\Delta_i]}{1 + \lambda E[\Delta_i]} P_i^{s/a} \right]$$

**Short setup period**

# Steady-state model

- Energy usage of active interfaces

$$\frac{P_i - q_i^z P_i^z}{1 - q_i^z} = \left[ \rho_i P_i^a + \frac{1 - \rho_i}{1 + \lambda E[\Delta_i]} P_i^s + \frac{\lambda(1 - \rho) E[\Delta_i]}{1 + \lambda E[\Delta_i]} P_i^{s/a} \right]$$

# Steady-state model

- M/G/1(E,SU) model
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$$\overline{W}_i = E[w_k | i] = \frac{\lambda E[S_i^2]}{2(1 - \rho_i)} + \frac{2E[\Delta_i] + \lambda E[\Delta_i^2]}{2(1 + \lambda E[\Delta_i])},$$

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$$\frac{P_i - q_i^z P_i^z}{1 - q_i^z} = \left[ \rho_i P_i^a + \frac{1 - \rho_i}{1 + \lambda E[\Delta_i]} P_i^s + \frac{\lambda(1 - \rho) E[\Delta_i]}{1 + \lambda E[\Delta_i]} P_i^{s/a} \right]$$

# Protocol optimization

- M/G/1(E,SU) model
  - Optimized eBond
  - Optimized eeeBond
- High-level summary
  - Theorems/lemmas specifying interface selection

# Protocol optimization

- M/G/1(E,SU) model
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THEOREM 1. *Given an average target waiting time  $W^*$  and an estimated packet inter arrival rate  $\lambda$ , the optimal eBond policy always picks the interface with the lowest service rates  $\mu_i$  that can support a packet arrival rate*

$$\lambda \leq \lambda_i^* = \frac{2(W^* - E[S_i])}{E[S_i^2] + 2E[S_i](W^* - E[S_i])}, \quad (10)$$

where  $E[S_i] = \frac{E[l_k]}{\mu_i}$  and  $E[S_i^2] = \frac{E[l_k^2]}{\mu_i^2}$ .

# Protocol optimization

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THEOREM 1. Given an average target waiting time  $W^*$

and  $\Delta_i$ ,  
 LEMMA 1. The expected waiting time  $W_i$  is a monotonically non-decreasing function of the arrival rate  $\lambda$  for the region in which  $W_i \geq \Delta_i$ , and for any  $\lambda \leq \lambda^*$  for which  $W_i^* = W_i(\lambda^*) \geq \Delta_i$ , the waiting time  $W_i(\lambda) \leq W_i(\lambda^*)$ .

$$E[S_i^2] + 2E[S_i](W^* - E[S_i])$$

where  $E[S_i] = \frac{E[l_k]}{\mu_i}$  and  $E[S_i^2] = \frac{E[l_k^2]}{\mu_i^2}$ .

# Protocol optimization

- M/G/1(E,SU) model
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THEOREM 1. Given an average target waiting time  $W^*$

and  $W_i = w_i(\lambda) \leq \Delta_i$ , the waiting time  $w_i(\lambda) \leq w_i(\lambda)$ .

LEMMA 1. The expected waiting time  $W_i$  is a monotonically non-increasing function of the service rate  $\mu_i$ .

LEMMA 2. The expected waiting time  $W_i$  is a monotonically non-increasing function of the service rate  $\mu_i$ .

$$E[S_i^2] + 2E[S_i](W^* - E[S_i])$$

where  $E[S_i] = \frac{E[l_k]}{\mu_i}$  and  $E[S_i^2] = \frac{E[l_k^2]}{\mu_i^2}$ .

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THEOREM 1. *Given an average target waiting time  $W^*$*

LEMMA 1. *The expected waiting time  $W_i$  is a monoton-*

LEMMA 2. *The expected waiting time  $W_i$  is a monoton-*

LEMMA 3. *Given a target delay  $W^* \geq \Delta_i$ , unless there does not exist any interface with higher service rate, the optimal policy never picks a low-power interface with service rate  $\mu_i$  when the packet arrival rate  $\lambda$  exceeds an upper bound*

$$\lambda_i^u = \frac{-a_1 + \sqrt{a_1^2 - 4a_2a_0}}{2a_2}, \quad (14)$$

where  $a_2 = \Delta_i E[S_i](2W^* - \Delta_i) + \Delta_i E[S_i^2]$ ,  $a_1 = E[S_i^2] + 2E[S_i](W^* - \Delta_i) + \Delta_i(\Delta_i - 2W^*)$ , and  $a_0 = 2(\Delta - W^*)$ .

# Protocol optimization

- M/G/1(E,SU) model
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<p>THEOREM 1. <i>Given an eBond interface selection policy, the expected power usage <math>P_i</math> is a monotonically non-decreasing function of the service rate <math>\mu_i</math> whenever <math>E[S_i] &lt; W_i</math>.</i></p>	<p>LEMMA 4. <i>The expected power usage <math>P_i</math> is a monotonically non-decreasing function of the service rate <math>\mu</math> whenever the relative energy scaling parameter <math>x</math> satisfies the condition:</i></p> $x \geq x^* = \frac{\Delta_i + E[S_i]}{G + \lambda H}, \quad (15)$ <p>where <math>G = c + (1 + c)\Delta_i + (1 - c)E[S_i]</math>, <math>H = \Delta_i(\Delta_i + (1 - c)E[S_i])</math>, and <math>c = \frac{P_i^s}{P_i^a}</math>. Otherwise, the expected power usage <math>P_i</math> is a monotonically non-increasing function of <math>\mu</math>.</p>
<p>LEMMA 1. <i>The expected power usage <math>P_i</math> is a monotonically non-decreasing function of the service rate <math>\mu_i</math> whenever <math>E[S_i] &lt; W_i</math>.</i></p>	<p>LEMMA 2. <i>The expected power usage <math>P_i</math> is a monotonically non-decreasing function of the service rate <math>\mu_i</math> whenever <math>E[S_i] &lt; W_i</math>.</i></p>
<p>LEMMA 3. <i>There does not exist an optimal policy for a given service rate <math>\mu_i</math> when the relative energy scaling parameter <math>x</math> is less than <math>x^*</math>.</i></p>	<p>LEMMA 5. <i>The expected power usage <math>P_i</math> is a monotonically non-increasing function of the service rate <math>\mu</math> whenever the relative energy scaling parameter <math>x</math> is greater than <math>x^*</math>.</i></p>

where  $a_2 = \Delta_i E[S_i](2W^* - \Delta_i) + \Delta_i E[S_i^2]$ ,  $a_1 = E[S_i^2] + 2E[S_i](W^* - \Delta_i) + \Delta_i(\Delta_i - 2W^*)$ , and  $a_0 = 2(\Delta - W^*)$ .

# Protocol optimization

- M/G/1(E,SU) model
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<p>THEOREM 1. <i>Given an interface <math>i</math> and a policy <math>\pi</math>, the expected power usage <math>P_i</math> is a monotonic function of the service rate <math>\mu_i</math> when the packet arrival rate <math>\lambda</math> is less than a lower bound <math>\lambda_i^l</math>.</i></p>	<p>LEMMA 4. <i>The expected power usage <math>P_i</math> is a monotonic function of the service rate <math>\mu_i</math> when the packet arrival rate <math>\lambda</math> is less than a lower bound <math>\lambda_i^l</math>.</i></p>
<p>LEMMA 1. <i>The expected power usage <math>P_i</math> is a monotonic function of the service rate <math>\mu_i</math> when the packet arrival rate <math>\lambda</math> is less than a lower bound <math>\lambda_i^l</math>.</i></p>	<p>LEMMA 5. <i>Unless there does not exist another interface with higher service rate, the optimal policy never picks a low-rate, low-power interface with service rate <math>\mu_i</math> (over an interface with higher service rate) when the packet arrival rate <math>\lambda</math> is less than a lower bound <math>\lambda_i^l</math>.</i></p>
<p>LEMMA 2. <i>The expected power usage <math>P_i</math> is a monotonic function of the service rate <math>\mu_i</math> when the packet arrival rate <math>\lambda</math> is less than a lower bound <math>\lambda_i^l</math>.</i></p>	$\lambda_i^l = \frac{1}{H}(\Delta_i + E[S_i] - xG), \quad (18)$
<p>LEMMA 3. <i>There does not exist a policy that is optimal when the packet arrival rate <math>\lambda</math> is less than a lower bound <math>\lambda_i^l</math>.</i></p>	<p>where <math>G</math> and <math>H</math> are defined as in Lemma 4.</p>

where  $a_2 = \Delta_i E[S_i](2W^* - \Delta_i) + \Delta_i E[S_i^2]$ ,  $a_1 = E[S_i^2] + 2E[S_i](W^* - \Delta_i) + \Delta_i(\Delta_i - 2W^*)$ , and  $a_0 = 2(\Delta - W^*)$ .

# Protocol optimization

- M/G/1(E,SU) model
  - Optimized eBond
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<p>THEOREM 1. Given an arrival rate <math>\lambda</math> and service times <math>S_i</math> with mean <math>E[S_i]</math> and variance <math>\text{var}[S_i]</math>, the expected waiting time <math>W_i</math> is given by</p>	<p>LEMMA 4. The expected power usage <math>P_i</math> is a monotonic function of the arrival rate <math>\lambda_i</math> and the service times <math>S_i</math>.</p>	<p>LEMMA 5. Unless there does not exist another interface that satisfies both constraints, the optimal policy picks the highest capacity interface.</p>
<p>LEMMA 1. The expected waiting time <math>W_i</math> is given by</p>	<p>LEMMA 3. The optimal policy does not exist when the arrival rate <math>\lambda_i</math> is greater than the service rate <math>\mu_i</math>.</p>	<p>THEOREM 2. Given a target waiting time <math>W^* \geq \max_i \Delta_i</math> and arrival rate <math>\lambda</math>, the optimal eeeBond policy picks the lowest powered interface that satisfy both (i) <math>\lambda_i^l \leq \lambda</math>, and (ii) <math>\lambda \leq \lambda_i^u</math>, where <math>\lambda_i^l</math> and <math>\lambda_i^u</math> are given by equations (18) and (14), respectively. In the case no interface satisfies both constraints, the optimal policy picks the highest capacity interface.</p>

where  $a_2 = \Delta_i E[S_i](2W^* - \Delta_i) + \Delta_i E[S_i^2]$ ,  $a_1 = E[S_i^2] + 2E[S_i](W^* - \Delta_i) + \Delta_i(\Delta_i - 2W^*)$ , and  $a_0 = 2(\Delta_i - W^*)$ .

# Protocol optimization

- M/G/1(E,SU) model
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**Given target waiting time  $W^*$  and arrival rate  $\lambda$ , which interface?**

THEOREM 1. Given an eBond interface  $\lambda_i$  and a target waiting time  $W^* \geq \max_i \Delta_i$ , the optimal policy picks the lowest capacity interface that satisfies both (i)  $\lambda_i \geq \lambda$ , and (ii)  $\lambda_i < \lambda_i^u$ , where  $\lambda_i$  and  $\lambda_i^u$  are given by equations (18) and (19).

LEMMA 1. The expected power usage  $P_i$  is a monotonic function of the arrival rate  $\lambda_i$ .

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LEMMA 4. The expected power usage  $P_i$  is a monotonic function of the arrival rate  $\lambda_i$ .

LEMMA 5. Unless there does not exist another interface  $\lambda_j$  that satisfies both (i)  $\lambda_j \geq \lambda$ , and (ii)  $\lambda_j < \lambda_j^u$ , where  $\lambda_j$  and  $\lambda_j^u$  are given by equations (18) and (19).

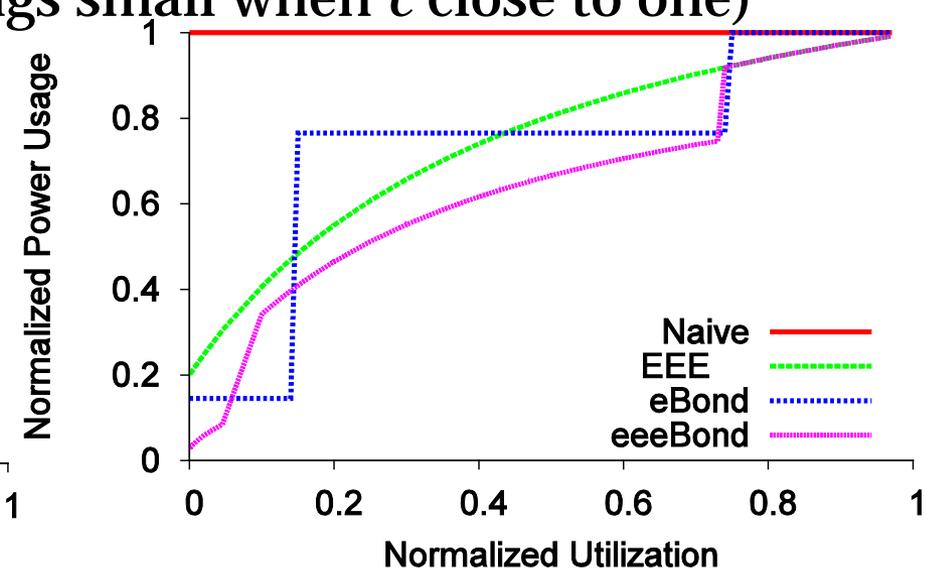
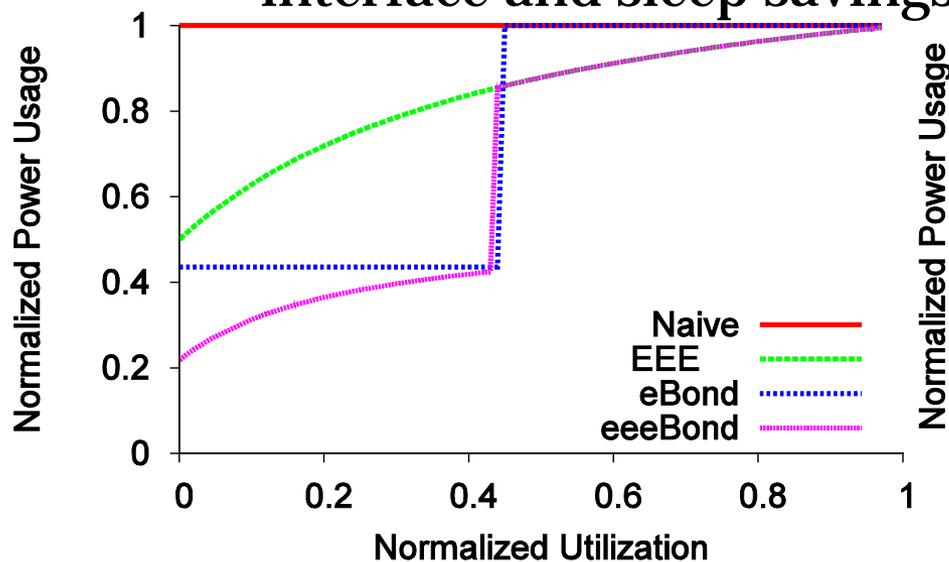
THEOREM 2. Given a target waiting time  $W^* \geq \max_i \Delta_i$  and an arrival rate  $\lambda$ , the optimal eBond interface  $\lambda_i$  that satisfies both (i)  $\lambda_i \geq \lambda$ , and (ii)  $\lambda_i < \lambda_i^u$ , where  $\lambda_i$  and  $\lambda_i^u$  are given by equations (18) and (19), is the highest capacity interface that satisfies both constraints.

where  $P_i$  is the expected power usage of interface  $i$ .

where  $a_2 = \Delta_i E[S_i](2W^* - \Delta_i) + \Delta_i E[S_i^2]$ ,  $a_1 = E[S_i^2] + 2E[S_i](W^* - \Delta_i) + \Delta_i(\Delta_i - 2W^*)$ , and  $a_0 = 2(\Delta_i - W^*)$ .

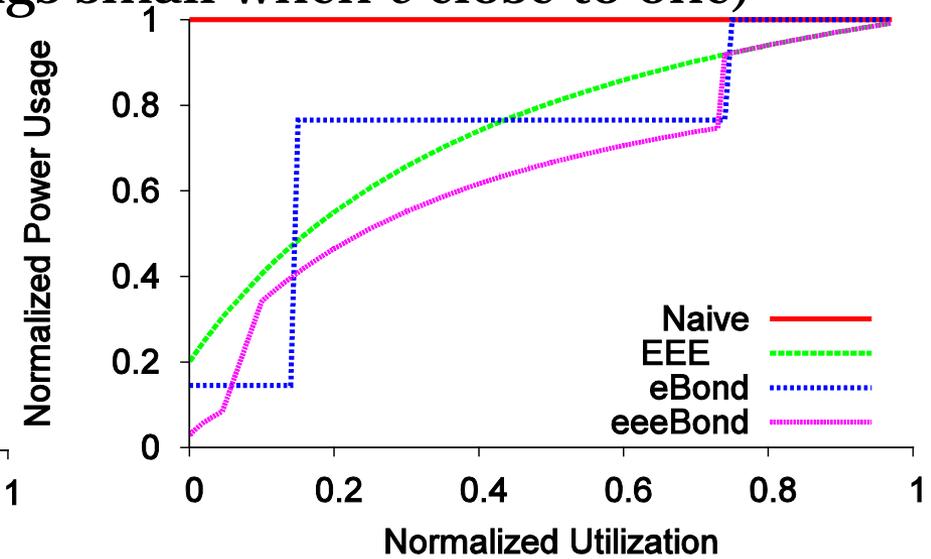
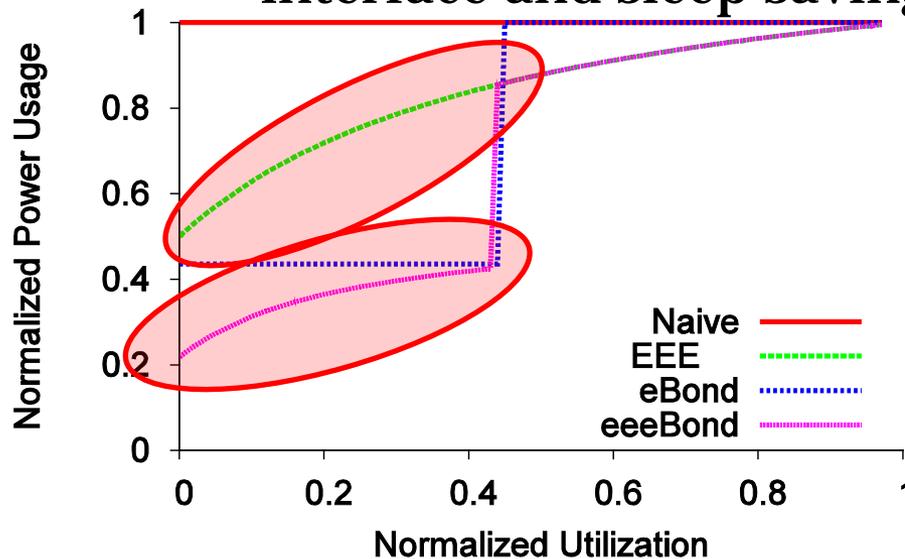
# Example scenarios

- EEE and eeeBond adopt power usage for individual interface(s)
- eeeBond often the winner, but cases where eBond even better
  - increase in delay prevent eeeBond using lower-power interface and sleep savings small when  $c$  close to one)



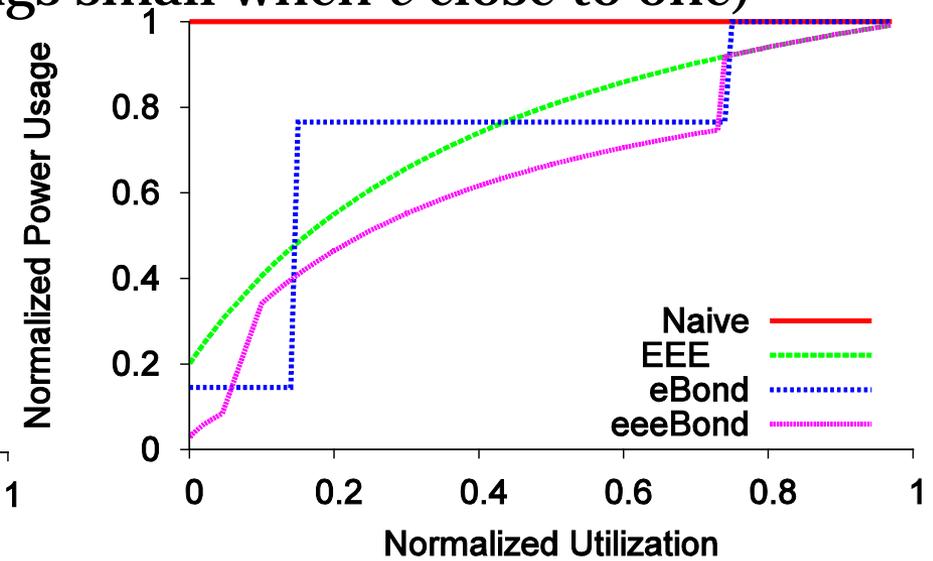
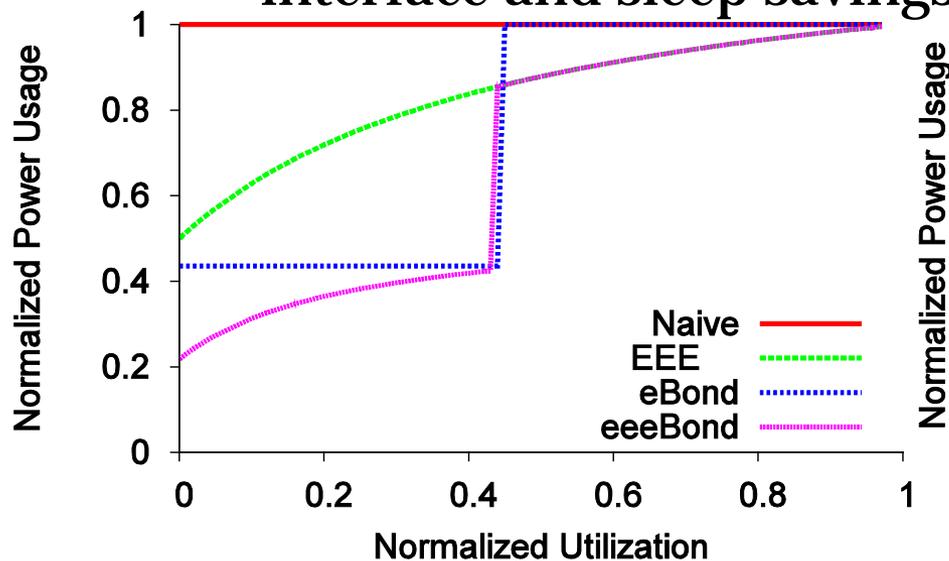
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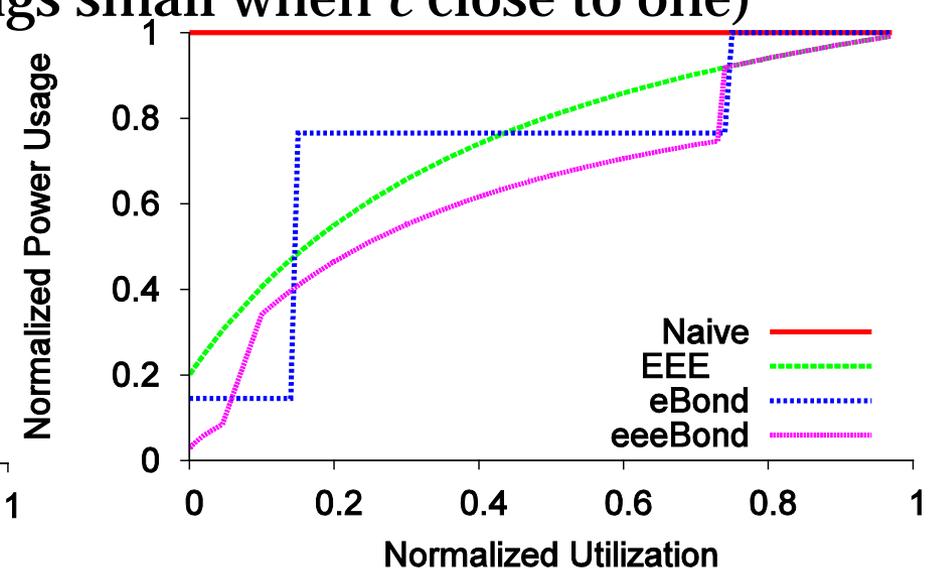
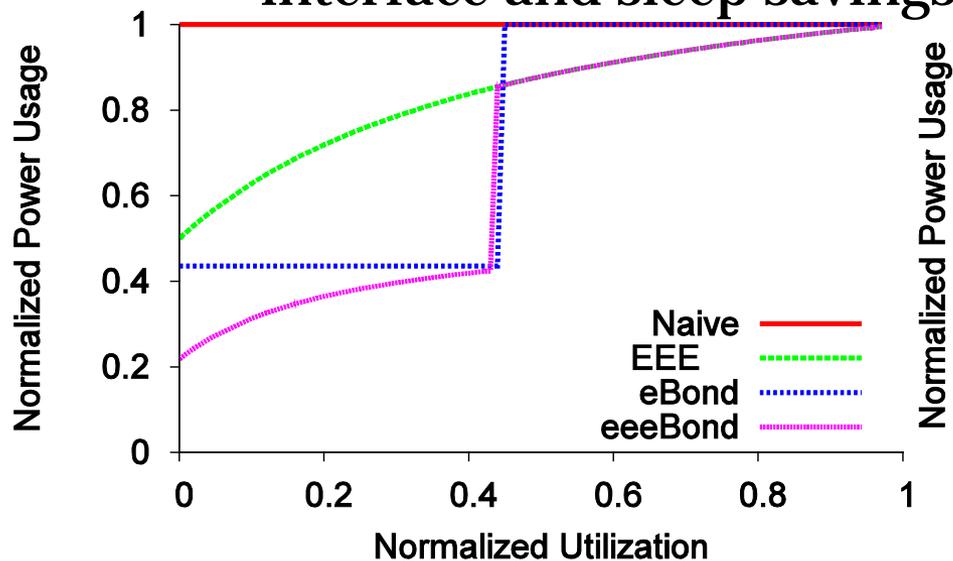
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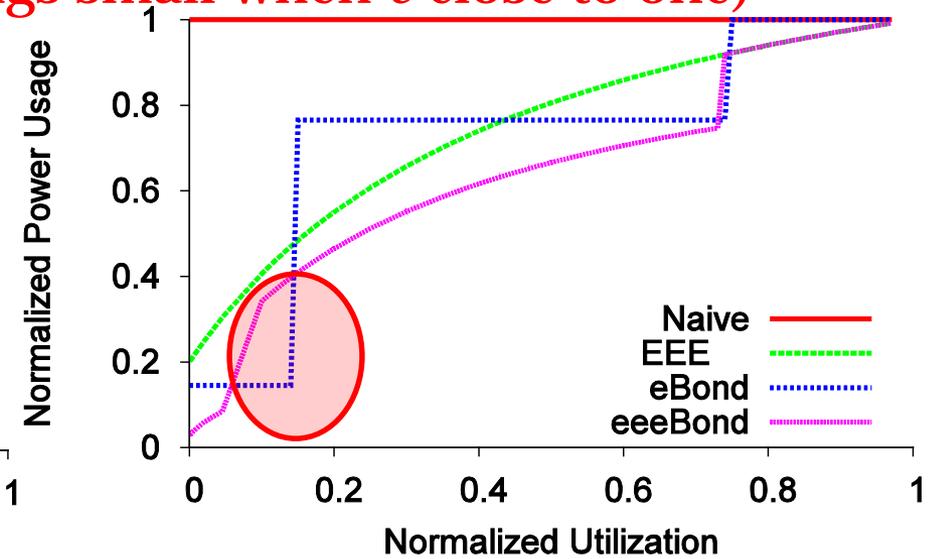
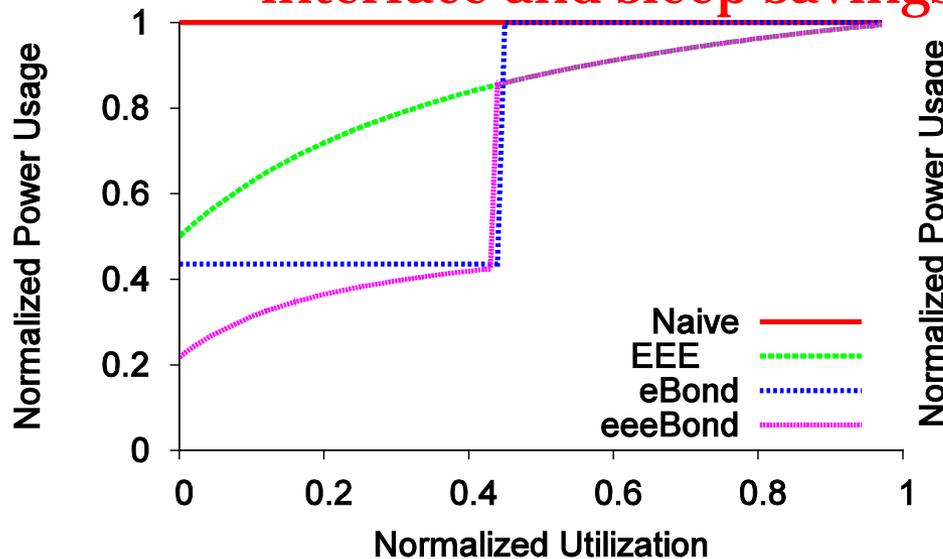
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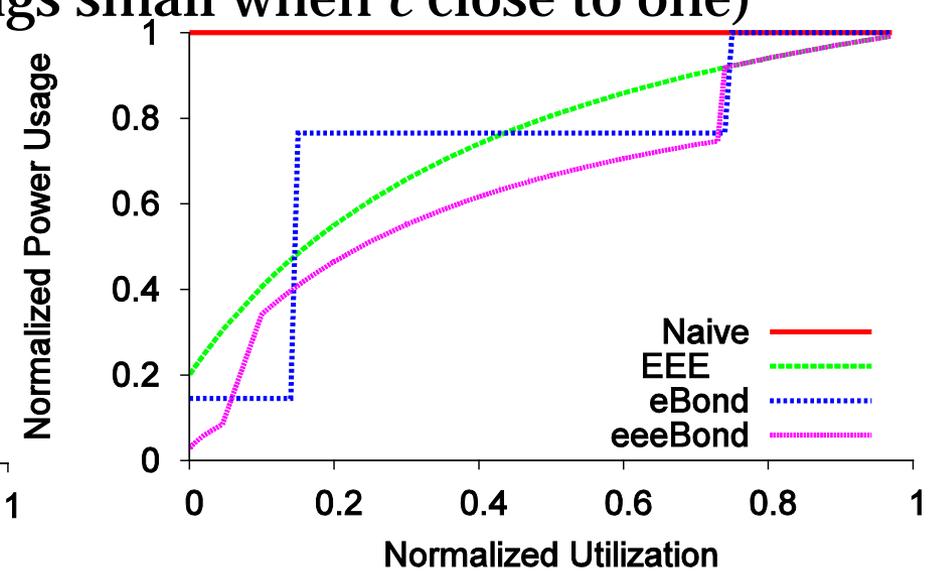
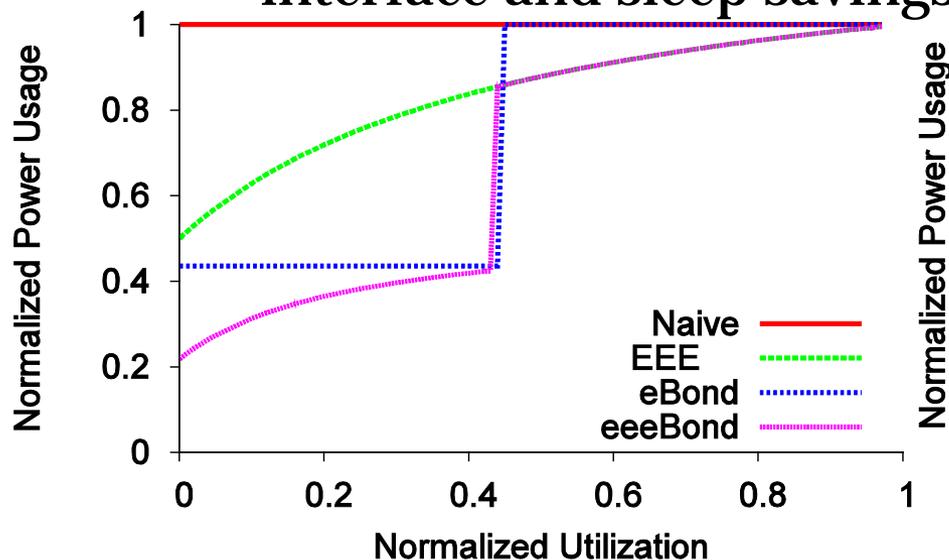
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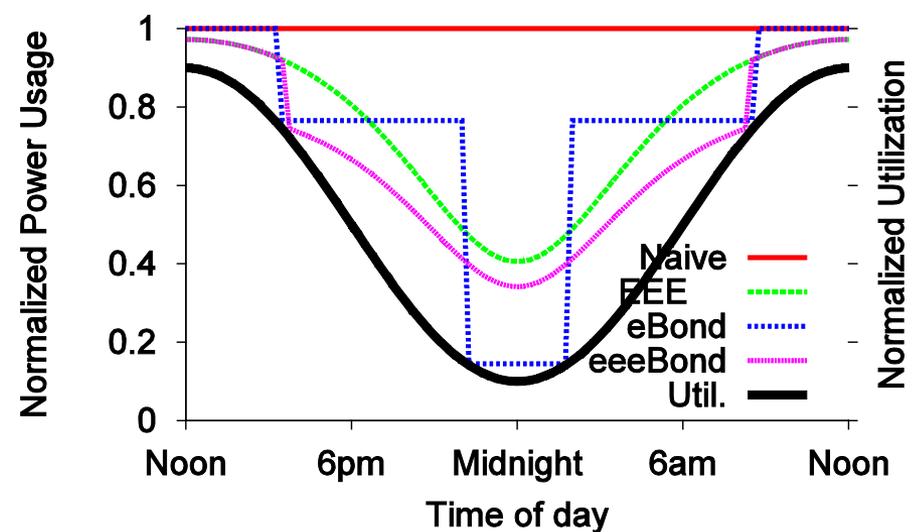
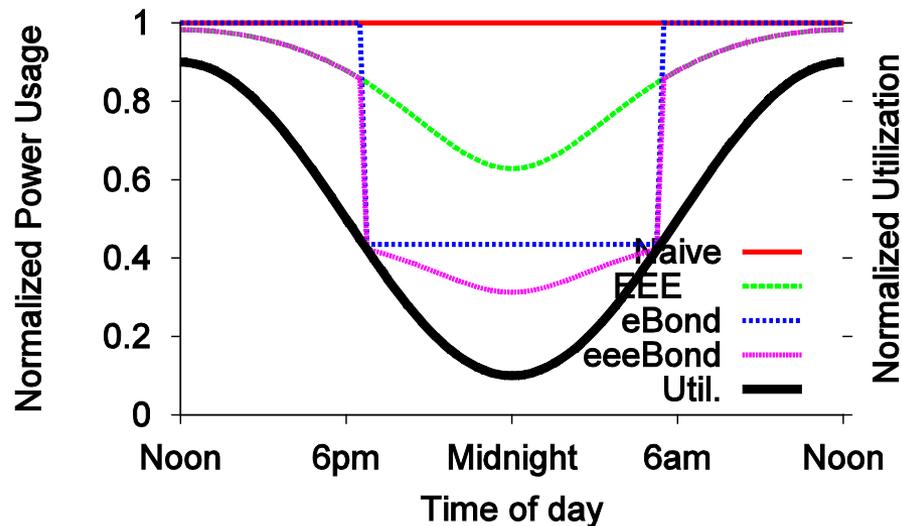
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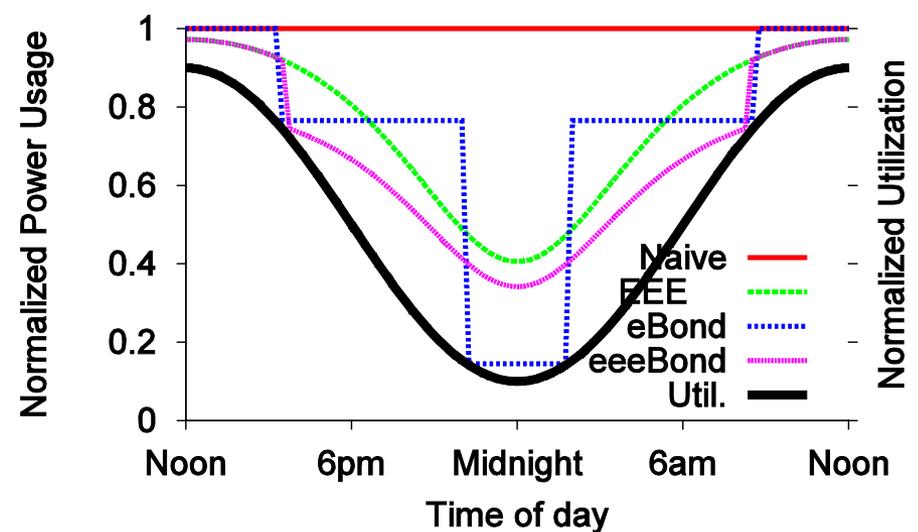
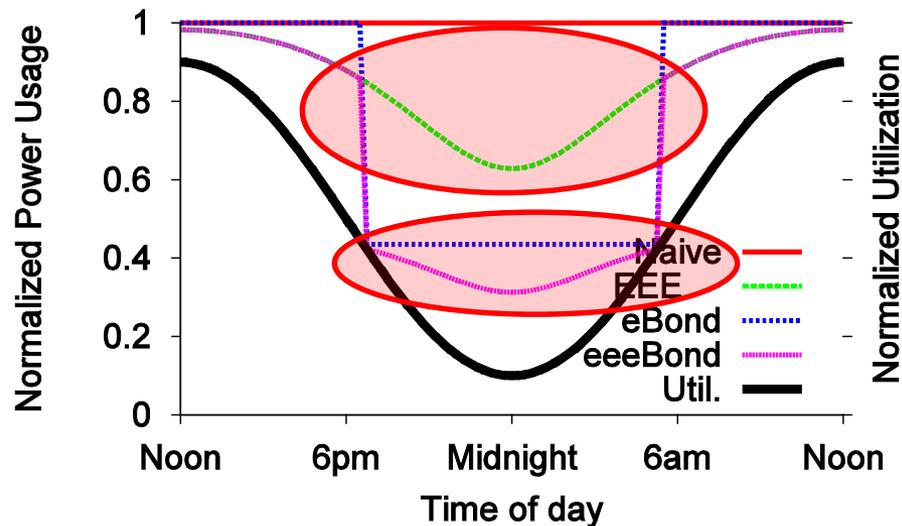
# Time-of-day comparison

- EEE and eeeBond adopt power usage for individual interface(s)
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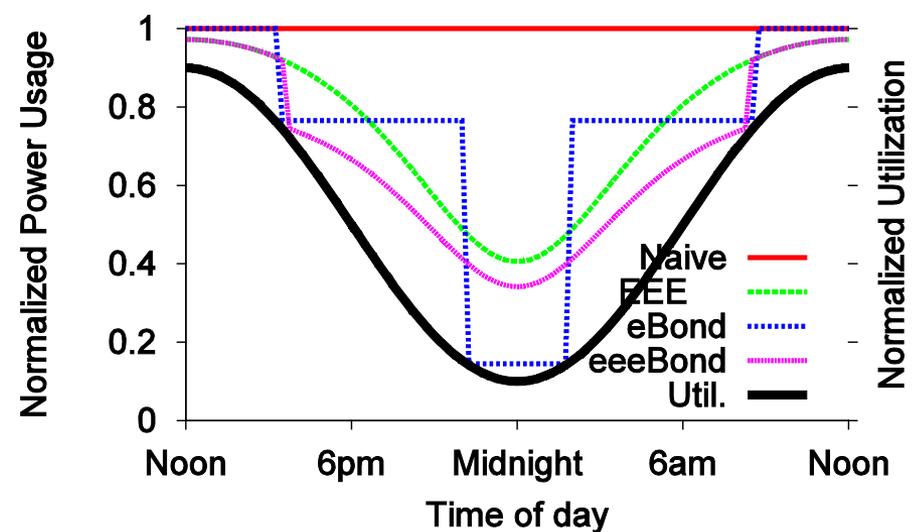
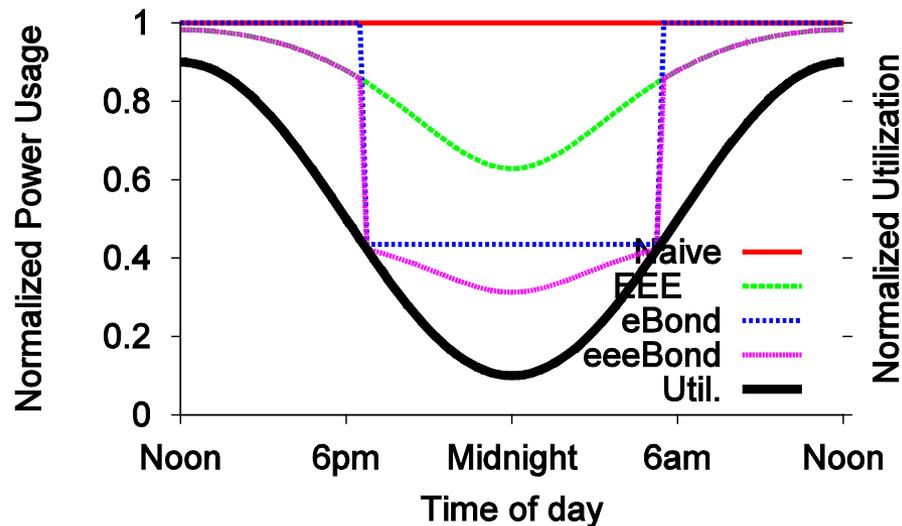
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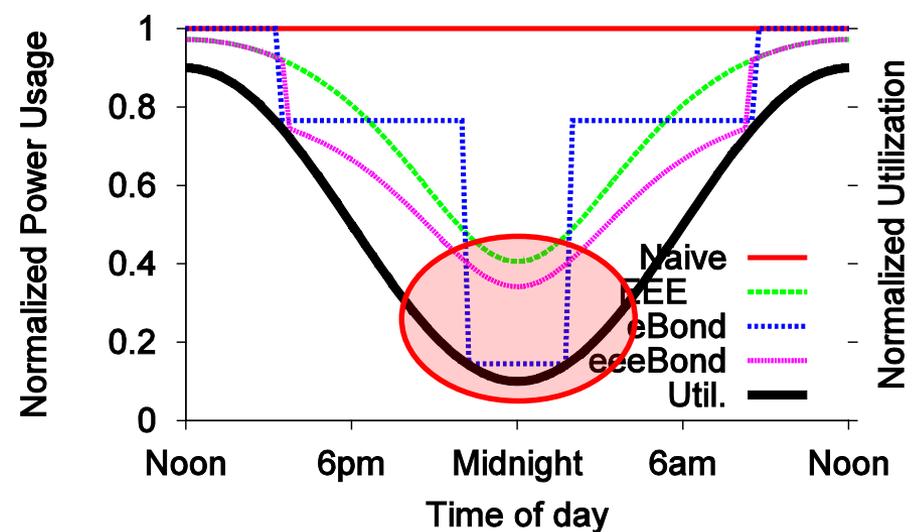
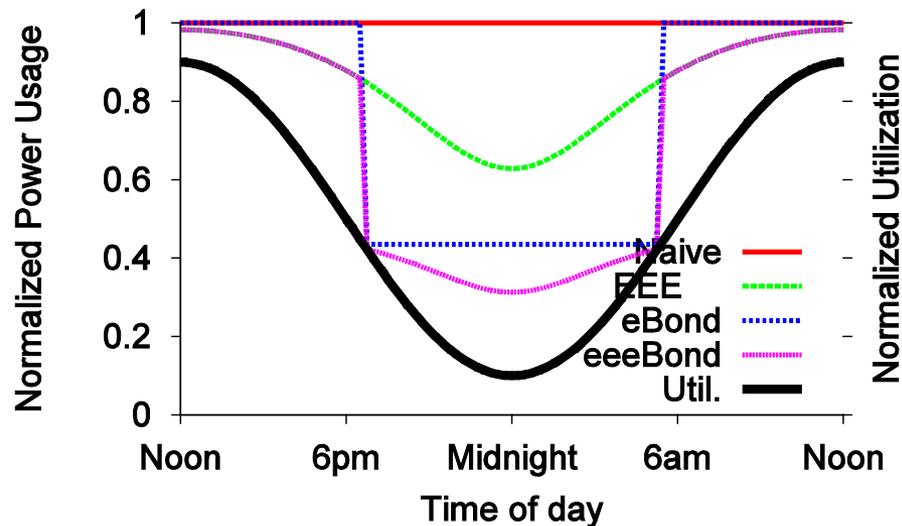
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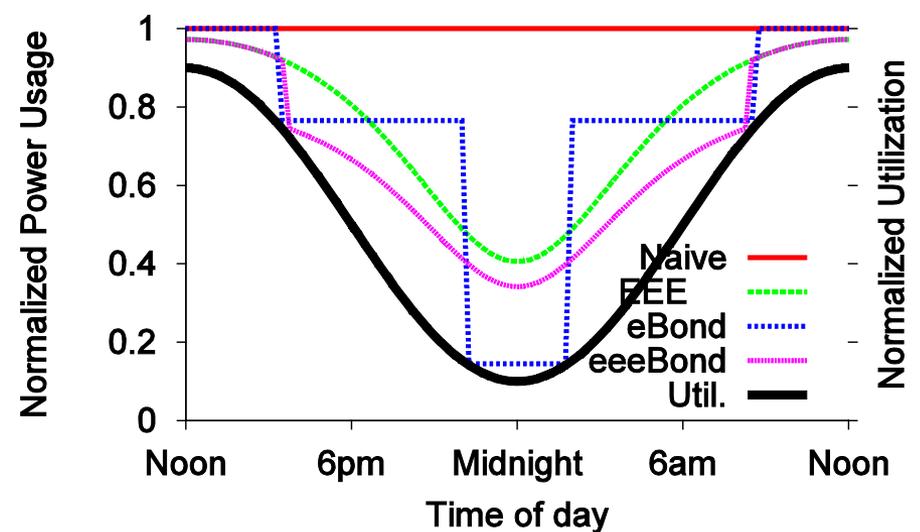
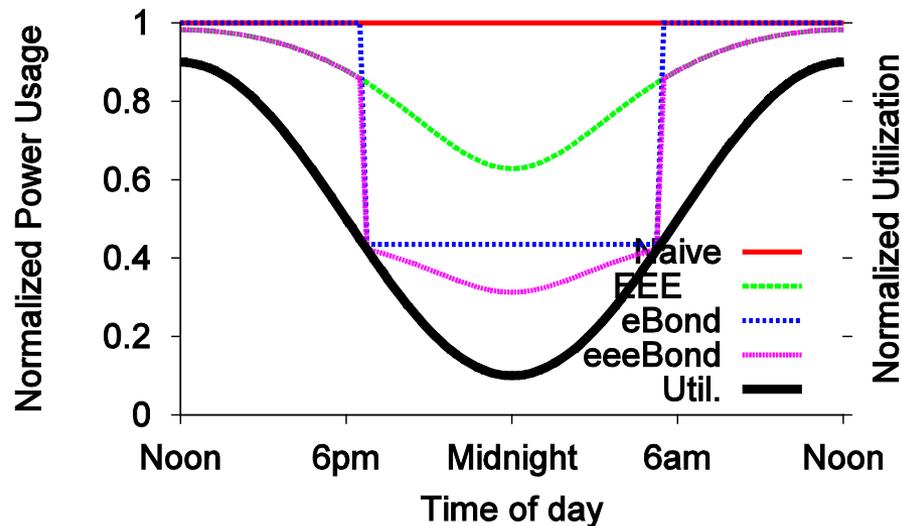
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- EEE and eeeBond adopt power usage for individual interface(s)
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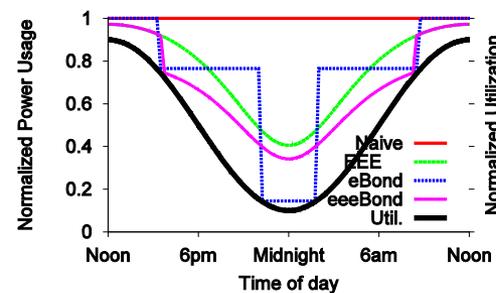
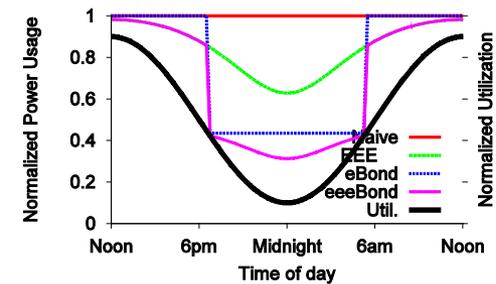
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# Normalized power usage with diurnal model

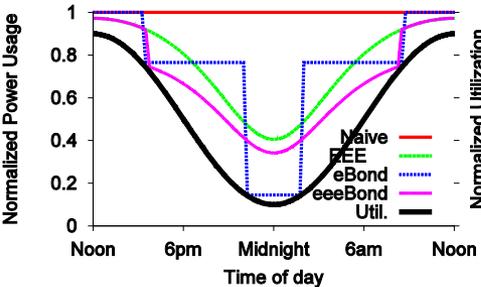
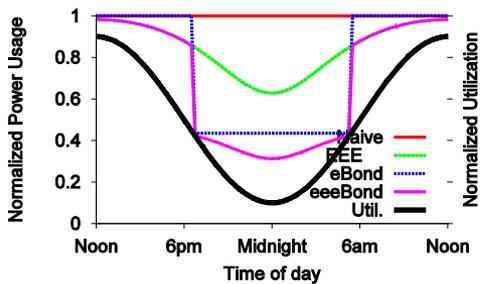
- eBond outperforms EEE (sometimes even eeeBond)
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Scenario		Current $c = 0.8$			Future $c = 0.2$			
		$\bar{u}$	$x$	EEE	eBond	$e^3B$	EEE	eBond
Two	0.5	1.2	0.95	0.76	<b>0.73</b>	0.76	0.76	<b>0.65</b>
	0.25	1.2	0.90	<b>0.49</b>	0.49	0.58	0.49	<b>0.38</b>
	0.125	1.2	0.87	0.44	<b>0.39</b>	0.44	0.44	<b>0.25</b>
	0.25	0.8	0.90	0.62	<b>0.60</b>	0.58	0.62	<b>0.47</b>
	0.25	2	0.90	<b>0.32</b>	0.34	0.58	0.32	<b>0.27</b>
Three	0.5	1.2	0.95	<b>0.74</b>	0.81	0.76	0.74	<b>0.68</b>
	0.25	1.2	0.90	<b>0.57</b>	0.59	0.58	0.57	<b>0.45</b>
	0.125	1.2	0.87	<b>0.43</b>	0.47	0.44	0.43	<b>0.30</b>
	0.25	0.8	0.90	<b>0.66</b>	0.67	0.58	0.66	<b>0.51</b>
	0.25	2	0.90	<b>0.45</b>	0.48	0.58	0.45	<b>0.36</b>

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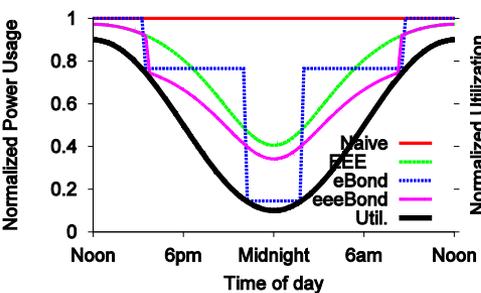
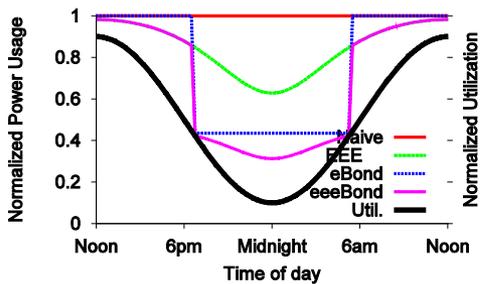
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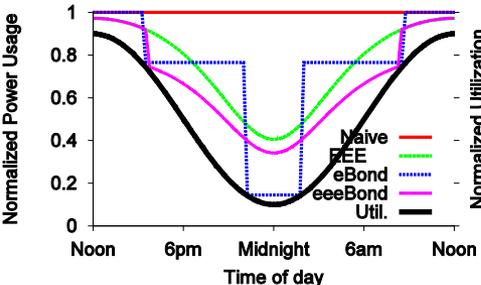
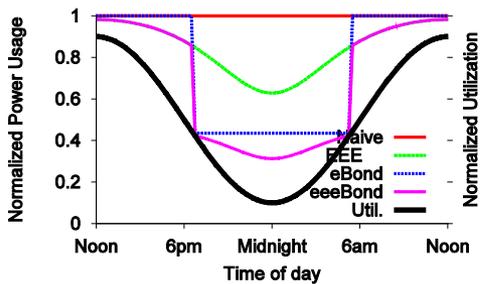
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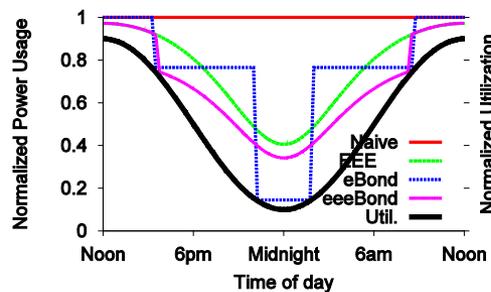
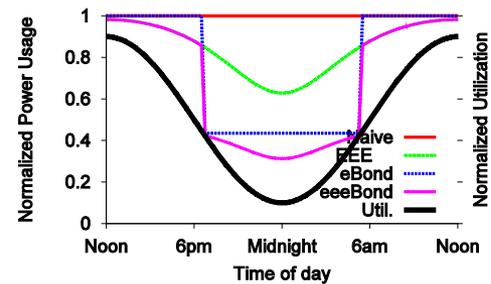
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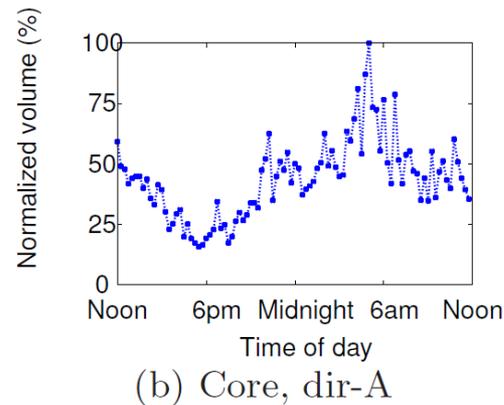
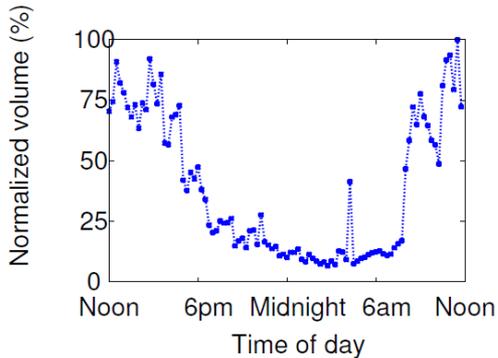
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# Trace-driven simulations

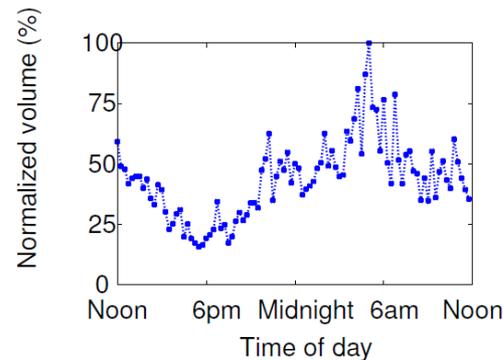
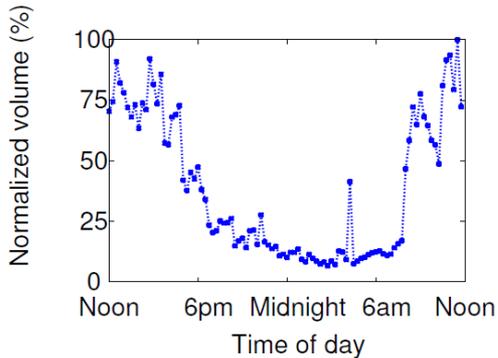
- eBond (and eeeBond) always better than EEE
- eeeBond has significant benefits over others when greater sleep benefits (i.e., smaller  $c$ )



Scenario		Current $c = 0.8$			Future $c = 0.2$		
		Trace	EEE	eBond	$e^3B$	EEE	eBond
Two	Edge, in	0.81	<b>0.16</b>	0.43	0.22	0.16	<b>0.13</b>
	Edge, out	0.81	<b>0.38</b>	0.74	0.22	0.38	<b>0.20</b>
	Core, dirA	0.81	0.15	<b>0.12</b>	0.21	0.15	<b>0.04</b>
	Core, dirB	0.82	0.15	<b>0.12</b>	0.24	0.15	<b>0.04</b>

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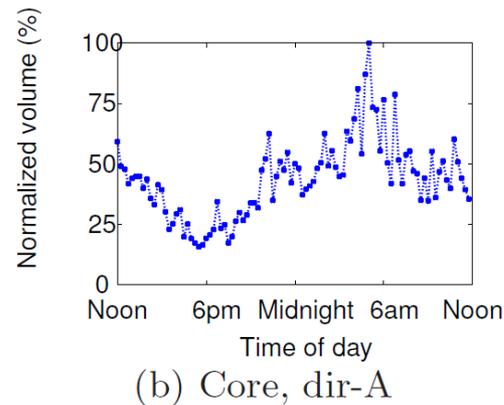
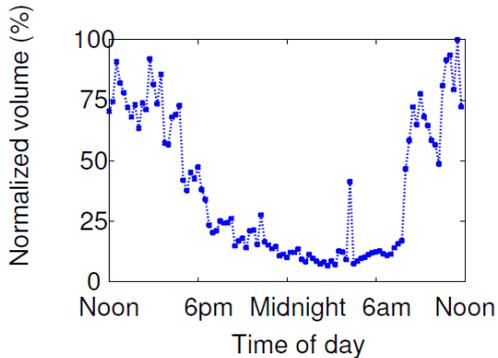
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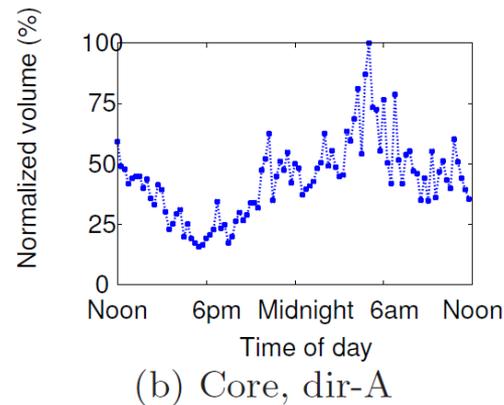
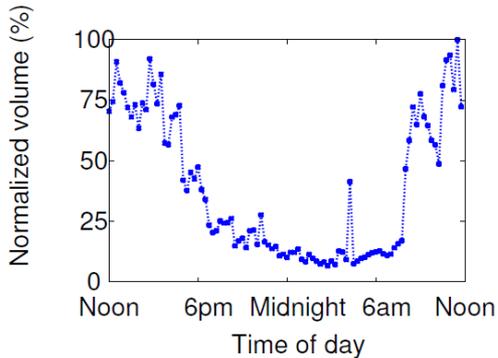
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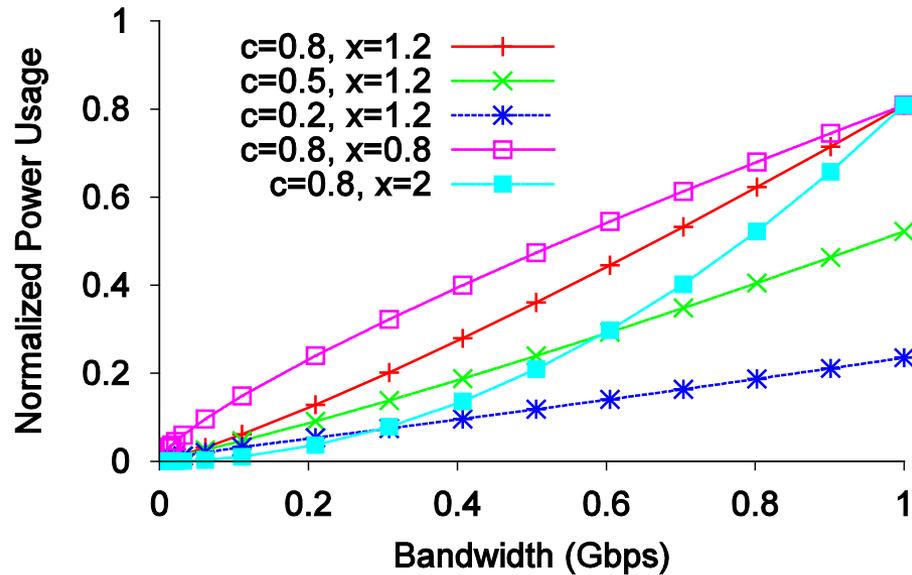
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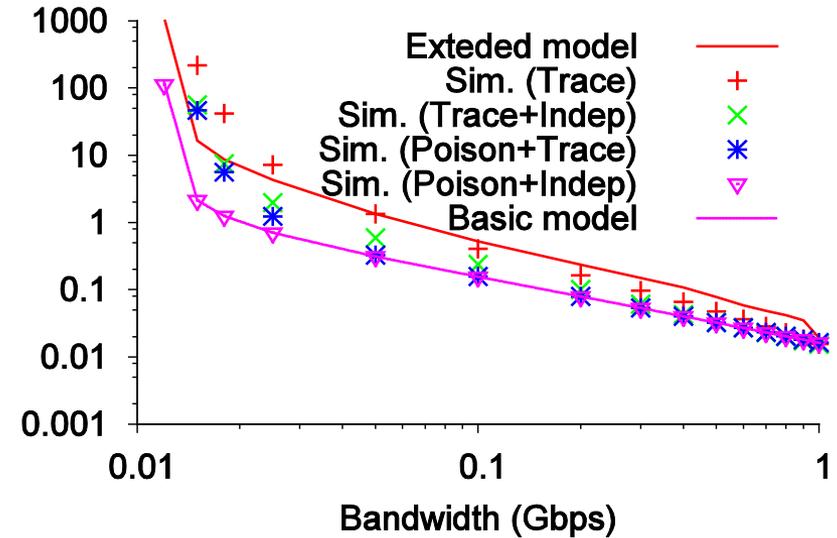


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# Model validation

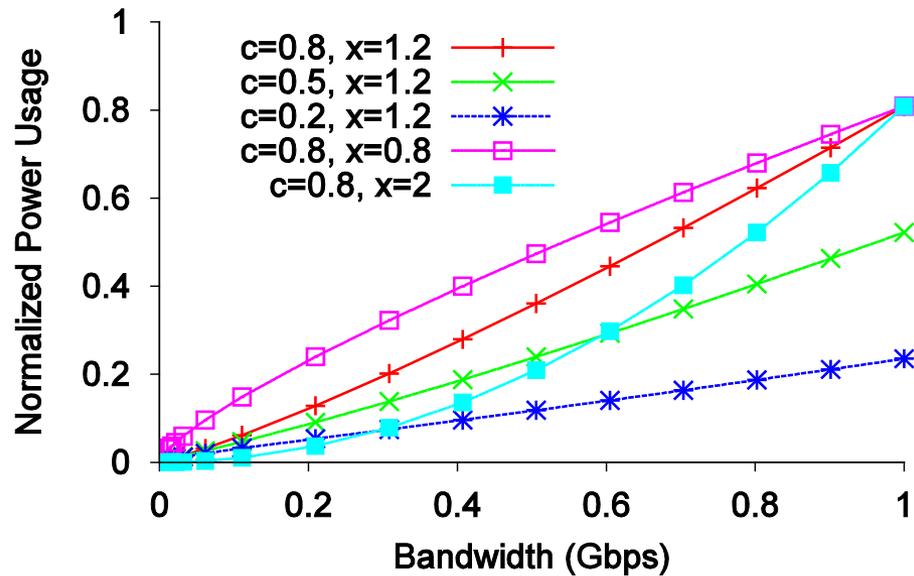


(a) Power model  
- Good match



(b) Delay model  
- Impact of assumptions  
- Extended model improves

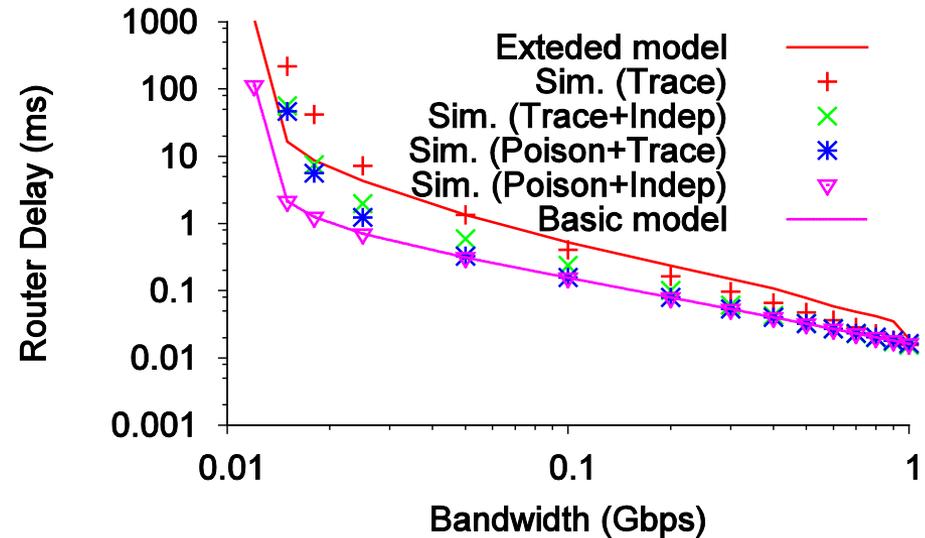
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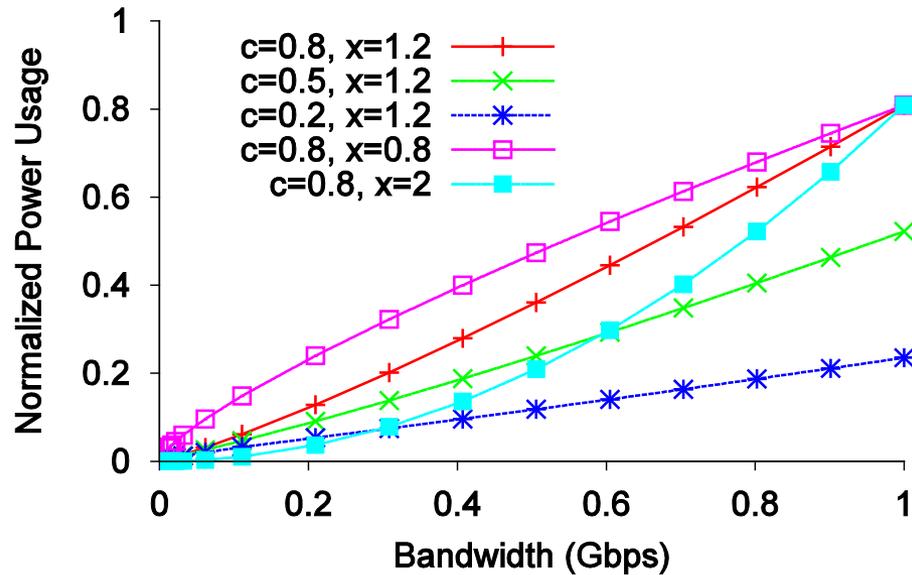
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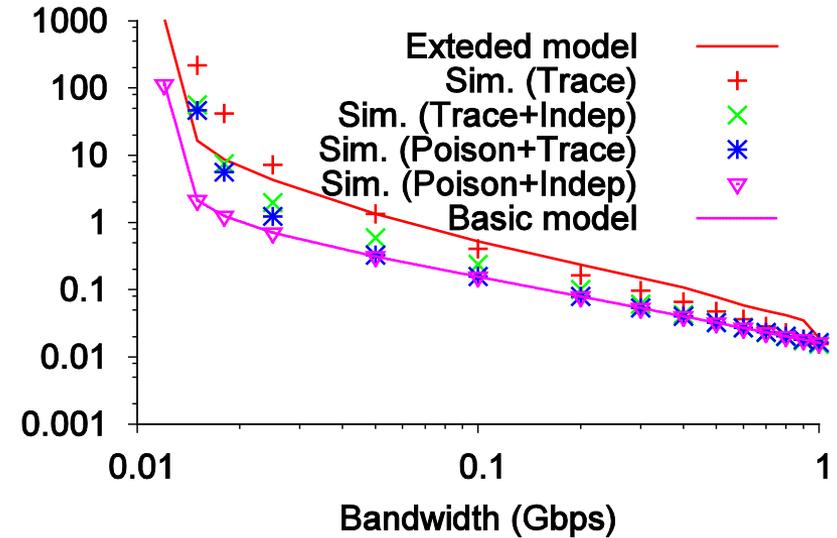
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(a) Power model  
- Good match



(b) Delay model  
- Impact of assumptions  
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# Conclusions

- Presented eeeBond
  - Hybrid protocol that combines benefits of EEE and eBond
- Presented a generalized protocol evaluation framework
- Performed protocol optimization of eBond and eeeBond
  - Closed-form expressions of delay and energy tradeoffs
- Characterized energy savings with the different protocols
  - Significant benefits of eBond and eeeBond over EEE (when  $x > 1$ ), even when EEE itself becomes more energy proportional
- Future work will refine our extended model and optimize additional aspects of eeeBond

# Optimized eeeBond: Energy Efficiency with non-Proportional Router Network Interfaces



Niklas Carlsson (niklas.carlsson@liu.se)